

An Application of C-language in Solving Minimum Spanning Connectivity of Clustered Cities to the Headquarter City

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Abstract: The primary objective of this article is to present a variant minimum spanning problem called “Minimum Spanning Connectivity of Clustered Cities to the Head Quarter City “which is a generalization of problem of Minimum Spanning Tree (MST) and to develop a Lexi-Search Approach(LSA) built on Pattern Recognition Technique(PRT) in order to solve the problem. Lexi Search Algorithms are shown to be dynamic in a large number of combinatorial situations. Here an innovative algorithm called LSA established on PRT has been proposed in order to acquire the optimal solution and the discussions made here are demonstrated by means of numerical examples. Using C- Language the proposed algorithm is designed and it can be observed that this algorithm has the ability to execute enormous problems.

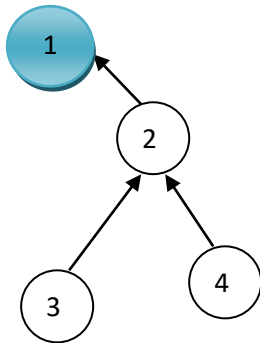
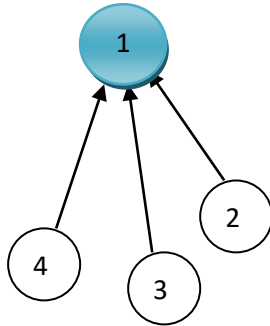
Keywords: Lexi-Search Approach (LSA), Pattern Recognition Technique (PRT), Distance Matrix, Feasible and Infeasible Solutions, Search Table.

I. INTRODUCTION

One major theme in clustering research over the past two decades has been the automatic classification of quantitatively described objects, without any constraint as to which pairs of such objects might ultimately find themselves in the same class. A second major trend in clustering work has been where there is such an inherent or an imposed representational constraint. This second area of clustering arises naturally in the analysis of point patterns, and lately it has become an increasing interest in the analysis of data in the Geo-sciences. Even though the objectives of

contiguity-constrained clustering algorithms may differ in pattern recognition, image processing, urban and regional studies, psychometrics, and so on, underlying principles are often shared, and valuable lessons may be learnt from other disciplines for the design of new algorithms.

Suppose a set $N = \{1, 2, 3, 4\}$ of cities whose distances ($N \times N$) are specified. The three cities have to connect to the Headquarter city $\{1\}$. When each city is individually connected, the total connectivity cost/distance is $d(2, 1) + d(3, 1) + d(4, 1)$ as shown in fig-1. When it is connected as shown in fig-2 the connectivity is sum of $d(2, 1)$, $d(3, 2)$ and $d(4, 2)$.



II. PROBLEM DESCRIPTION

Suppose there is a set of some cities N . The distance between any two cities of them is also known. Among them city '1' consider a head quarter. A few cities of them are considered as a set of sub head quarter cities. The remaining cities of them are converted in to different groups of cities. The number of groups must be less than number of cities in set of sub head quarter cities. The cities in any two groups are distinct and cities in each group with set of sub head quarter cities are also distinct. The aim of the problem is to connect groups of cities to head quarter city through a sub head quarter cities with minimum total distance/cost. Here, the restriction of the problem is cities of any group are connected to any one sub head quarter city either directly or indirectly.

Let there be a set of 'n' cities defined as $N = \{1, 2, 3, \dots, n\}$. Here city '1' can be considered as head quarter. The distance between any two cities is denoted as $D(i, j)$ in matrix form, where $i, j \in N$. Let SH be a set of 'q' cities as sub head quarter cities denoted as $SH = \{\alpha_1, \alpha_2, \alpha_3, \dots, \alpha_q\}$, where $SH \subset N$. The remaining $n-(q+1)$ cities formed as $G_1, G_2, \dots, G_p$ of 'p' groups of distinct cities, where $n-(q+1) = |G_1| + |G_2| + \dots + |G_p|$. Here $G_i \cap G_j = \emptyset$,

where i is not equal to j and $i, j = 1, 2, 3, \dots, p$. The aim of the problem is to connect groups of cities to head quarter city through some sub head quarter cities with minimum total distance/cost. Here the restriction of the problem is cities of any group are connected to any one sub head quarter city only either directly or indirectly.

III. MATHEMATICAL FORMULATION

$$|N| = n, |SH| = q, \quad 1 \in N$$

$$|G_1| = g_1, |G_2| = g_2, \dots, |G_p| = g_p, G_i \subset N, \sum_{i=1}^p g_i = g, SH \subset N$$

$$(SH) \cap (UG_i) = \emptyset \text{ and } G_i \cap G_j = \emptyset, i \neq j.$$

$$i, j = 1 \text{ to } p$$

$$\text{Min } Z = \sum_{i \in N} \sum_{j \in N} D(i, j) X(i, j) \dots \dots \dots (1)$$

$$\sum_{j \in SH} X(j, 1) = p \dots \dots \dots (2)$$

$$X(i, j) = 0 \quad \text{if } i \in G_s, j \in G_t \quad \text{where } s \neq t; \\ s, t = 1, 2, \dots, p \dots \dots \dots (3)$$

$$\sum_{i \in N} \sum_{j \in N} X(i, j) = (g + p) - 1 \dots \dots \dots (4)$$

$$\sum_{i \in G_s, j \in G_s \cup \{\alpha\}} X(i, j) = g_s, \text{ where } \alpha \in SH \\ \& \ s = 1, 2, 3, \dots, p \dots \dots \dots (5)$$

$$X(i, j) = 1 \text{ or } 0 \dots \dots \dots (6)$$

Equation (1) represents the objective of the problem, i.e., minimize the distance/cost.

Equation (2) denotes number of groups formed from the cities of set SH ($q > p$).

Equation (3) indicates there is no connectivity between any two cities of two different groups.

Equation (4) states total number of connectivity must be equal to sum of total cities in all groups and number of groups.

Equation (5) shows number of connectivity formed from a group to a sub head quarter city.

Equation (6) represents if a city 'i' connected to city 'j' is 1, otherwise 0.

IV. NUMERICAL FORMULATION

The improvised concepts and algorithm are exemplified by an algebraic example in which cities total no. is $N = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$. In the example, given below first the optimal solution in Lexi-search approach using the "Pattern Recognition Technique" from cities to the head quarter is derived. City "1" is considered the head quarter. The distance (i, i) is considered ∞ and also disconnectivity to the matching cities. $D(i, j)$'s considered natural numbers. The distance matrix $D(i, j)$ is appearing in **Tab-1**

Tab – 1

		1	2	3	4	5	6	7	8	9	10
D (i,j)	1	∞	∞	∞	∞	∞	∞	∞	∞	∞	∞
	2	∞	∞	7	13	∞	7	2	∞	8	∞
	3	4	∞	∞	∞	∞	∞	∞	∞	∞	∞
	4	∞	6	15	∞	∞	4	8	∞	1	∞
	5	∞	∞	2	∞	∞	∞	3	14	4	9
	6	∞	14	10	6	∞	∞	6	∞	11	∞
	7	3	∞	∞	∞	∞	∞	∞	∞	∞	∞
	8	∞	∞	13	∞	5	∞	12	∞	5	14
	9	9	∞	∞	∞	∞	∞	∞	∞	∞	∞
	10	∞	∞	7	∞	12	∞	3	10	15	∞

Here we considered city 1 as head quarter, city 3, city 7, city 9 as sub head quarters defined as $SH = \{3, 7, 9\}$, first group consists of cities 2, 4, 6 mentioned as $G_1 = \{2, 4, 6\}$ and second group consists of cities 5, 8, 10 denoted by $G_2 = \{5, 8, 10\}$. The objective of the problem is that the cities of two groups should connect to head quarter city 1 through few cities in SH (sub head quarter) with minimum distance.

Hence $D(4, 2) = 6$

V. FEASIBLE SOLUTION

Suppose

$\{(4,9), (5,3), (3,1), (8,5), (6,4), (2,6), (10,3), (9,1)\}$

represents feasible solution. The following **fig-1** signifies the above feasible solution. The diamond shape represents headquarter, hexagon shape represents sub headquarter cities and rectangle shape represents groups which consists of cities that are represented by the circles. Value at arc epitomizes distance/cost between the respective two cities.

From the below **figure-1**, first group of cities are connected to headquarter city through the sub headquarter city 9 in such a way that cities 2 and 6 are mapped and cities 6 and 4 are mapped then city 4 is mapped to head quarter through sub headquarter city 9. The second group of cities are connected to headquarter city through sub headquarter city 3 in such a way that city 8 is mapped to city 5 and city 5 is mapped to head quarter through sub headquarter city 3. City 10 is connected directly to the headquarter city through sub headquarter city 3. The distance/cost is

$Z =$

$D(4,9) + D(5,3) + D(3,1) + D(8,5) + D(6,4) + D(2,6) + D(10,3) + D(9,1)$

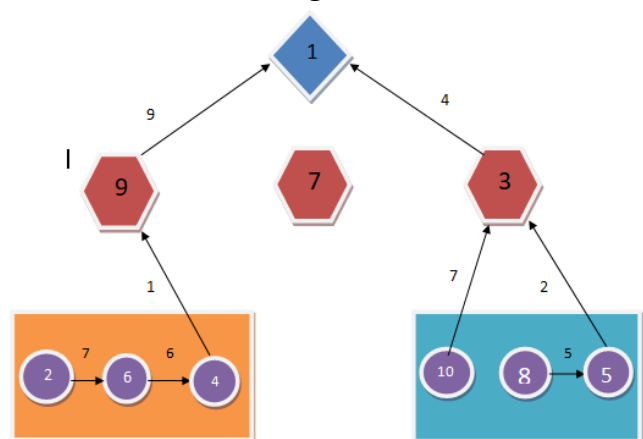
$= 1 + 2 + 4 + 5 + 6 + 7 + 7 + 9$

$= 41$

The total distances = 41 unit

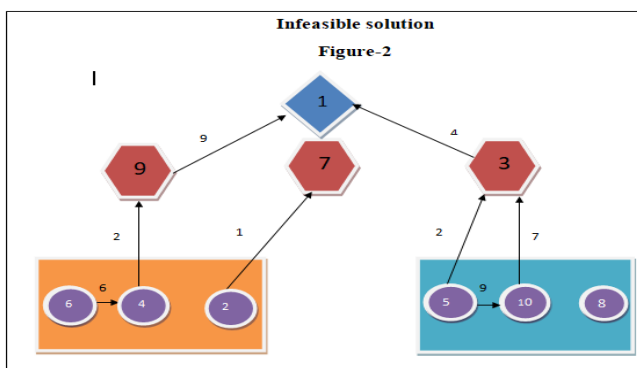
Feasible solution

Figure-1



VI. INFEASIBLE SOLUTION

The collection $\{(4,9),(2,7),(5,3),(3,1),(6,4),(10,3),(5,10),(9,1)\}$ represents an infeasible solution for minimum spanning network connectivity from cities to the head quarter. **Fig-2** is an infeasible solution. The diamond shape gives headquarter, hexagon shape means sub headquarter cities and rectangle shape represents groups which consists of cities represented by circles. Entries at arc denotes distance/cost between the respective two cities. Consider a set ordered pairs $\{(4,9),(2,7),(5,3),(3,1),(6,4),(10,3),(5,10),(9,1)\}$ represents an infeasible solution. From the below **Fig-2**,



in first group, city 4 is associated to sub headquarter city 9 and city 2 is connected to sub headquarter city 7, according to the hypothesis, the cities in a group should be connected to the headquarter city through one sub headquarter city only. Initially, city 4 is in first group, connected to sub headquarter city 9. In the same way, city 2 should be connected to sub headquarter city 9. But here, the city 2 is connected to sub headquarter city 7 has indicated an infeasible solution. Further in second group, city 5 is mapped to the sub headquarter city 3 and mapped to city 10 which is also an infeasible solution. According to hypothesis, cities in a group should be connected to the headquarter through the subheadquarter city only once either directly or indirectly. Here, city 5 is connected to sub headquarter 3 and connected from city 10 that indicated infeasible solution to this problem. The distance/cost is

$$\begin{aligned} Z &= D(4,9) + D(2,7) + D(5,3) + D(3,1) + D(6,4) + D(10,3) + D(5,10) + D(9,1) \\ &= 1 + 2 + 2 + 4 + 6 + 7 + 9 + 9 \\ &= 40. \end{aligned}$$

The total distances = 40 units.

VII. ALGORITHMS

```
STEP0: IX = 0          GOTO1
STEP1: IS (IR (RA) = 1) IF YES GOTO 17
              IF NO GOTO 2
STEP2: GR = G (RA); GC = G (CA) GOTO 3

STEP3: IS (GR = GC) IF YES GOTO 4
              IF NO GOTO 5
STEP4: IS (GR = 1) IF YES GOTO 17
              IF NO GOTO 12
STEP5: IS (GC = 0) IF YES GOTO 6
              IF NO GOTO 7
STEP6: IS (GR = 1) IF YES GOTO 10
              IF NO GOTO 17
STEP7: IS (GC = 1) IF YES GOTO 8
              IF NO GOTO 17
STEP8: IS (CLR (GR) = 0) IF YES GOTO 15
              IF NO GO TO 9
STEP9: IS (CLR (GR) = CA) IF YES GOTO 16
              IF NO GOTO 17
STEP10: IS (KLR = P-2) IF YES GOTO 11
              IF NO GOTO 16
STEP11: IS (IC (RA) = 1) IF YES GOTO 16
              IF NO GOTO 17
STEP12: W=CA          GOTO 13
STEP13: IS [SW (W) =0] IF YES GOTO 16
              IF NO GO TO 14
STEP14: W=SW (W)
              IS (W=RA) IF YES GOTO17
              IF NO GOTO 13
STEP15: CLR (GR) = CA
              KLR=KLR+1GOTO 16
STEP16 : IX=1          GOTO 17
STEP17: STOP
```

ALGORITHM 2 (LEXI-SEARCH CALCULATION)

STEP0: Initialization

The arrays SN, R, C, D, DC, KA, KB, KC, P, Q, R, M, V, LB and values of N are made available. SA, DR and IK are initialized. The values $I=1$, $S=0$, $VT=9999$ and $Max = (n^2 - 2n - 1) - (p - 2)$

```
STEP1: S = S + 1
              IS(S > Max) IF YES GOTO 7
              IF NO GOTO 2
```

STEP2 : RA=R(S), CA=C(S)
V (I) = V (I-1) + D (S)
LB (I) = V (I) + DC (S+P-2 - I) – DC (S)
IS (LB (I) ≥ VT) IF YES GOTO 7
IF NO GOTO 3

STEP3: Check Feasibility using Algorithm 1

STEP4: IS (I = P-2) IF YES GOTO 6
IF NO GOTO 5

STEP5: IR (RA) = 1
IC (CA) = IC (CA) + 1
L (I) = S

SW (CA) = RA
Max = Max + 1, I = I+1 GO TO 1

STEP6: VT = V (I) = LB (I)
(Print the full length word)
Record VT GOTO 8

STEP7: IS (I = 1) IF YES GOTO 9
IF NO GOTO 8

STEP8: L (I) = 0, I = I-1
IR (RA) = 0
IC (CA) = IC (CA) - 1
SW (CA) = 0 GO TO 1

STEP9: STOP

VIII. SEARCH TABLE

The rules of receiving an optimal word using the above algorithm for the illustrative numerical example are given in the following Tab-2.

Tab-2

SN	1	2	3	4	5	6	7	8	V	L B	R	C	R E
1	1								1	2 2	4	9	A
2		2							3	2 2	2	7	R
3		3							3	2 4	5	3	A
4			4						6	2 4	5	7	R
5			5						6	2	7	1	R

										6			
6			6						6	2 8	1 0	7	R
7			7						7	3 1	3	1	A
8			8						1 1	3 1	4	6	R
9			9						1 1	3 3	5	9	R
10			1 0						1 2	3 5	8	5	A
11				1 1					1 7	3 5	8	9	R
12				1 2					1 8	3 7	4	2	R
13				1 3					1 8	3 8	6	4	A
14					1 4				2 4	3 8	6	7	R
15					1 5				2 5	3 9	2	3	R
16					1 6				2 5	4 0	2	6	A
17						1 7			3 2	4 0	1 0	3	A
18							1 8		4 0	4 0	2	9	R
19							1 9		4 0	4 0	4	7	R
20							2 0		4 1	4 1	5	1 0	R
21							2 1		4 1	4 1	9	1	A, = V T
22							1 8		3 3	4 1	2	9	R, = V T

23					1 7			2 5	4 1	1 0	3	R, = V T
24				1 4				1 8	3 9	6	7	R
25				1 5				1 9	4 1	2	3	R, = V T
26			1 1					1 2	3 7	8	9	R
27			1 2					1 3	3 9	4	2	R
28			1 3					1 3	4 0	6	4	A
29				1 4				1 9	4 0	6	7	R
30				1 5				2 0	4 2	2	3	R, = V T
31			1 4					1 3	4 2	6	7	R, = V T
32		8						7	3 3	4	6	R
33		9						7	3 5	5	9	R
34		1 0						8	3 8	8	5	A
35			1 1					1 3	3 8	8	9	R
36			1 2					1 4	4 0	4	2	R
37			1 3					1 4	4 1	6	4	R, = V T

38			1 1							8	4 0	8	9	R
39			1 2							9	4 2	4	2	R, = V T
40		4								4	2 7	5	7	A
41			5							7	2 7	7	1	A
42				6						1 0	2 7	1 0	7	A
43					7					1 4	2 7	3	1	R
44					8					1 4	2 8	4	6	R
45					9					1 4	3 0	5	9	R
46					1 0					1 5	3 2	8	5	A
47						1 1				2 0	3 2	8	9	R
48						1 2				2 1	3 3	4	2	R
49						1 3				2 1	3 4	6	4	A
50							1 4			2 7	3 4	6	7	R
51							1 5			2 8	3 5	2	3	R
52							1 6			2 8	3 5	2	6	A
53								1 7		3 5	3 5	1 0	3	R
54								1 8		3 6	3 6	2	9	R
55								1 9		3 6	3 6	4	7	R

56							20	37	37	51	R
57							21	37	37	91	A, = V T
58						17		28	36	13	R
59						18		29	37	29	R, = V T
60					14			21	35	67	R
61					15			22	36	23	R
62					16			22	37	26	R, = V T
63				11				15	33	89	R
64				12				16	35	42	R
65				13				16	36	64	A
66					14			22	36	67	R
67					15			23	37	23	R, = V T
68				14				16	37	67	R, = V T
69			7					11	29	31	R
70			8					11	31	46	R

71				9					11	35	9R
72				10					12	38	5A
73					11				17	38	9R
74					12				18	37	42R, = V T
75				11					12	37	89R, = V T
76			6						7	29	17A
77				7					11	29	31R
78				8					11	31	46R
79				9					11	35	9R
80				10					12	38	5A
81					11				17	38	9R
82					12				18	37	42R, = V T
83				11					12	37	89R, = V T
84			7						8	32	31R
85			8						8	34	46R
86			9						8	36	59R

87			1 0						9	3 9	8	5	R, > V T
88		5							4	2 9	7	1	A
89			6						7	2 9	1 0	7	A
90				7					1 1	2 9	3	1	R
91				8					1 1	3 1	4	6	R
92				9					1 1	3 3	5	9	R
93				1 0					1 2	3 5	8	5	A
94					1 1				1 7	3 5	8	9	R
95					1 2				1 8	3 7	4	2	R, = V T
96				1 1					1 2	3 7	8	9	R, = V T
97			7						8	3 2	3	1	R
98			8						8	3 4	4	6	R
99			9						8	3 6	5	9	R
100				1 0					9	3 9	8	5	R, > V T
101		6							4	3 2	1 0	7	A
102			7						8	3 2	3	1	R

103			8							8	3 4	4	6	R
104			9							8	3 6	5	9	R
105				1 0						9	3 9	8	5	R, > V T
106		7								5	3 5	3	1	A
107			8							9	3 5	4	6	R
108				9						9	3 7	5	9	R, = V T
109		8								5	3 7	4	6	R, = V T
110	2									2	2 5	2	7	A
111		3								4	2 5	5	3	A
112			4							7	2 5	5	7	R
113			5							7	2 7	7	1	A
114				6						1 0	2 7	1 0	7	R
115				7						1 1	2 9	3	1	A
116					8					1 5	2 9	4	6	A
117						9				1 9	2 9	5	9	R
118						1 0				2 0	3 1	8	5	A
119							1			2	3	8	9	R

						1		5	1			
120						1 2		2 6	3 2	4	2	R
121						1 3		2 6	3 2	6	4	R
122						1 4		2 6	3 3	6	7	A
123							1 5	3 3	3 3	2	3	R
124							1 6	3 3	3 3	2	6	R
125							1 7	3 3	3 3	1 0	3	A, = V T
126						1 5		2 7	3 4	2	3	R, > V T
127						1 1		2 0	3 2	8	9	R
128						1 2		2 1	3 3	4	2	R, = V T
129				9				1 5	3 1	5	9	R
130				1 0				1 6	3 3	8	5	R, = V T
131			8					1 1	3 1	4	6	A
132				9				1 5	3 1	5	9	R
133				1 0				1 6	3 3	8	5	R, = V T
134			9					1	3	5	9	R,

										1	3		= V T
135			6							7	2 9	1 0	R
136			7							8	3 2	3 1	A
137				8						1 2	3 2	4 6	A
138					9					1 6	3 2	5 9	R
139						1 0				1 7	3 4	8 5	R, > V T
140				9						1 2	3 4	5 9	R, > V T
141			8							8	3 4	4 6	R, > V T
142		4								5	2 8	5 7	R
143		5								5	3 0	7 1	A
144			6							8	3 0	1 0	R
145			7							9	3 3	3 1	R, = V T
146		6								5	3 3	1 0	R, = V T
147	3									2	2 8	5 3	A
148		4								5	2	5 7	R

									8			
149	5							5	3	7	1	A
150		6						8	3	1	7	R
151		7						9	3	3	1	R, = V T
152		6						5	3	1	7	R, = V T
153	4							3	3	5	7	A
154		5						6	3	7	1	A
155		6						9	3	1	7	A
156			7					1	3	3	1	A
157				8				1	3	4	6	A
158					9			2	3	5	9	R
159					1			2	3	8	5	R, = V T
160				9				1	3	5	9	R, = V T
161			8					1	3	4	6	R, = V T
162		7						1	3	3	1	R, > V

												T
163		6						6	3	1	7	R, > V T
164	5							3	3	7	1	R, > V T

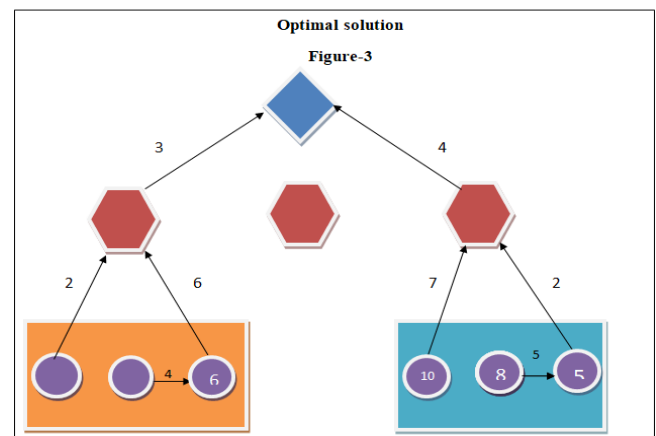
IX. COMMENTS

Tab – 6, provides optimal solution with the optimal word is **L₈ = (2, 3, 5, 7, 8, 10, 14, 17)**. Optimal solution at final state **VT** is **33** at final state which is appearing in the **125th** row and the corresponding ordered pairs are **(2,7),(5,3),(7,1),(3,1),(4,6),(8,5),(6,7),(10,3)**.

Tab– 3

	1	2	3	4	5	6	7	8	9	10
L	2	3	5	7	8	10	14	17	-	-
IR	-	1	1	1	1	1	1	1	-	1
IC	1+1	-	1+1	-	1	1	1+1	-	-	-
SW	-	7	1	6	3	7	1	5	-	3

The ordered pairs set **{(2,7), (5,3), (7,1), (3,1), (4,6), (8,5), (6,7), (10,3)}** represents an optimal solution.



From the above **Fig-3**, the first group of cities are connected to the headquarter city through a sub headquarter city 7, in such a way, that city 2 is connected to the headquarter through a sub headquarter 7. City 4 is mapped to city 6 and city 6 is mapped to the head quarter through a sub headquarter city 7. Similarly, second group of cities are connected to the headquarter city through a sub headquarter city 3, in such a way, that city 8 is mapped to city 5 and city 5 is mapped to the head quarter through a sub headquarter city 3. City 10 is connected to the headquarter city through a sub headquarter city 3. The distance/cost

$$Z = D(2,7) + D(5,3) + D(7,1) + D(3,1) + D(4,6) + D(8,5) + D(6,7) + D(10,3) \\ = 2 + 2 + 3 + 4 + 4 + 5 + 6 + 7 \\ = 33$$

The total distances = 33 units.

Consider an ordered pair set $\{(2,7), (5,3), (7,1), (3,1), (4,6), (8,5), (6,7), (10,3)\}$, which is a feasible solution

tab-4

$$X(i, j) = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

X. Experimental Results and Comparison Details

The table given below displays the computational results for Lexi-Search algorithm using PRT. H= Head quarter, SH = number of sub headquarters, P = the number of groups/clusters, G₁, G₂ and G₃ are groups/clusters some cities.

Table-5

S. No	No. of cities	No. of clusters	Published model	Proposed model
1	18	3	0.879121	0.8432
2	20	3	1.703386	0.8655
3	22	3	0.76923	0.7593
4	25	3	1.923077	0.9124

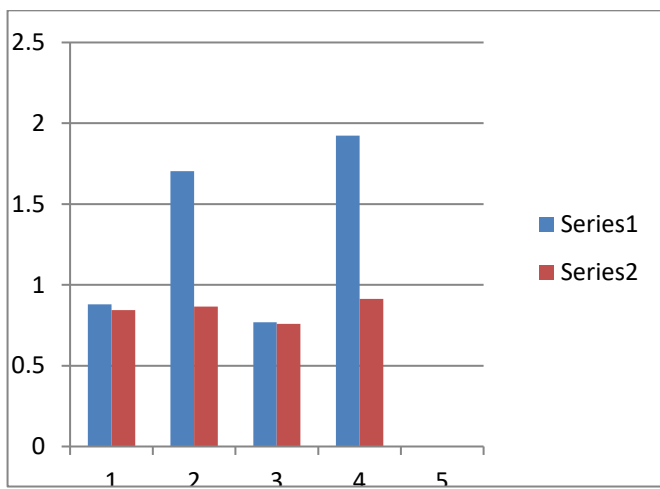
Table – 6

SN	N	H	SH	P			VT	CPU Run Time in seconds
				G1	G2	G3		Avg. AT + ST
1	5	1	2	2	-	-	35	0.0000
2	6	1	2	2	2	-	47	0.0000
3	8	1	3	2	2	-	54	0.0000
4	9	1	3	3	2	-	62	0.1234
5	9	1	3	2	3	-	65	0.1586
6	10	1	3	4	2	-	179	0.2357
7	10	1	3	3	3	-	142	0.2531
8	10	1	3	2	4	-	156	0.3258
9	11	1	3	2	3	2	194	0.5493
10	11	1	3	3	2	2	172	0.6123

11	12	1	3	3	2	3	185	0.6349
12	15	1	4	3	4	3	189	0.7352
13	18	1	5	4	5	3	196	0.8432
14	20	1	5	4	5	5	201	0.8655
15	22	1	6	5	6	4	224	0.7593
16	25	1	7	6	6	5	247	0.9124

In the graph given below second series characterize that CPU run time to achieve optimal solution by proposed model and first series denote that CPU run time for examining the optimal solution by the published model. Moreover the proposed model receives less time than published model in presenting the solution.

GRAPH-1



Using this series2 gives CPU run time to obtain optimal solution by proposed model and series 1 gives CPU run time for examining the optimal solution by the published model. Also the proposed model assumes less time than published model for giving the solution.

XI. CONCLUSION AND FUTURE RESEARCH

In the above discussion an exact algorithm called LSA (Lexi-Search Algorithm) built on PRT

(Pattern Recognition Technique)has been presented in order to solve the **MINIMUM SPANNING CONNECTIVITY OF CLUSTERED CITIES TO THE HEADQUARTER CITY**. LSAs have been shown to be more effective in a large number of combinatorial situations. At initial stage a model is framed into a 0-1 programming phenomena and then an LSA based on PRT is established for obtaining an optimal solution. The problem is exemplified with appropriate numerical example. Using C-language the algorithm is proposed and the calculations are reported and compared with the existing results. One can observe that to obtain an optimal solution the CPU run time is reasonably less for higher values of the problem than the published model. Using these results one can strongly contemplate that the proposed algorithm can perform larger size problems. In the context of future research two problems namely Vehicle Routing Problem with Inter-Loading Facilities and a Variant Constraint Bulk Transshipment Problem can be proposed and analyzed by means of C-Language

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