

Real Power Minimization with Voltage Profile Enhancement Using Series and Shunt FACTS Controllers – Sine Cosine Algorithm Approach

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Abstract

Proper management of reactive power resources is essential for the secure and stable functioning of power systems in the standpoint of voltage stability. The main purpose of optimal reactive power dispatch (ORPD) is to detect the settings of control variables such as the voltage rating of generators, reactive power injection of VAR compensators and tap ratios of the tap setting transformers in order to decrease the grid congestion with one or more objective of minimizing the active power loss for a fixed economic power schedule while taking on a given set of constraints. In this paper, Flexible AC Transmission System (FACTS) controllers named as Static Var Compensator (SVC) and Thyristor Controlled Series Capacitor (TCSC) are added to the conventional ORPD problem for active power loss minimization with voltage profile improvement. As well, this report presents the application of sine cosine algorithm (SCA) to find the optimal solution of ORPD (with and without FACTS devices) of power arrangement with different examination systems (Standard IEEE 14-bus, IEEE 57-bus and IEEE 118-bus) with distinct cases such as minimization of active power losses and improvement of voltage profile. Simulation results demonstrate the high tone and accuracy of the proposed algorithm, and considering the quality of the solution obtained, the proposed algorithm appears to be efficient and robust to solve the ORPD problem (with and without FACTS devices) comparing with existing literatures.

Keywords: *Optimal reactive power dispatch, Active power Loss reduction, Improvement of voltage profile, FACTS devices, Sine cosine algorithm, Whale optimization algorithm, Ant lion optimizer*

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1. Introduction

In the final few decades, optimal reactive power dispatch (ORPD) has received great attention and it has become a tool for improving the economy and security of power system performance. The ORPD, which is a non-linear, non-convex and non-differentiable optimization problem, aims at minimizing the objective functions such as voltage stability and system real power losses via adjustments of control parameters like generator voltages, switchable volt-ampere reactive (VAR) sources,

transformer tap settings and so on in a power system while satisfying equality and inequality constraints [1-3].

Agreeing to the literature, mathematical algorithms such as Decomposition method, Newton approach, non-linear programming, interior point, Jacobian matrix etc. have been used for ORPD solutions initially [4-7]. These algorithms optimize the objective function by linearizing it. Since the ORPD problem has local optima more than one, it is a non-linear and multi-modal optimization problem. Hence, it is so tough to determine the global optimum using mathematical algorithms in the resolution

of the ORPD problem. However, in that respect are some disadvantages specially to the algorithms such as insecure convergence and algorithmic complexity. For these

causes, researchers were developed heuristic and meta heuristic based algorithms for solving the ORPD problem was shown in Table. 1.

Table 1: Summary of the proposed algorithms for solution of ORPD problem in literature

| Reference | Approach | Objective | Test System |
|--|-----------|---|---|
| Yan et al. (2004) [8] | IEP | Power loss | IEEE 118-bus system and a realistic power system in Western China |
| Zhao et al. (2005) [9] | MAPSO | Power loss | IEEE 30-bus and IEEE 118-bus |
| Varadarajan and Swarup(2008) [10] | DE | Power loss | IEEE 14, IEEE 30, and IEEE 118-Bus |
| Ying Li et al. (2009) [11] | DPSO | power loss and the costs of adjusting the control devices | IEEE 30-bus |
| Chaohua et al. (2009) [12] | SOA | Power loss | IEEE 57-bus and IEEE 118-bus |
| Mahadevan and Kannan(2010) [13] | CLPSO | Power loss and voltage profile | IEEE 30-bus and IEEE 118-bus |
| Xuexia Zhang et al., (2010) [14] | DMSDE | Power loss | IEEE 30-bus, IEEE 57-bus and IEEE 118-bus |
| Khazali and Kalantar (2011) [15] | HSA | Power loss and voltage profile | IEEE 30-bus and IEEE 57-bus |
| S. Jeyadevi et al. (2011) [16] | MNSGA-II | Power loss and voltage stability | IEEE 30-bus and IEEE 118-bus |
| Roy et al. (2012) [17] | BBO | Power loss and voltage profile | IEEE 30-bus and IEEE 118-bus |
| Xu et al. (2012) [18] | MASRL | Power loss | Ward-Hale 6-bus, IEEE 30-bus and IEEE 162-bus |
| S. Duman et al. (2012) [19] | GSA | Power loss, voltage profile, and voltage stability | IEEE 30-bus, IEEE 57-bus and IEEE 118-bus |
| R. Mallipeddi et al. (2012) [20] | HDE | Power loss and voltage profile | IEEE 30-bus, IEEE57-bus and IEEE 118-bus |
| Barun Mandal and Provas Kumar Roy (2013) [21] | QOTLBO | Power loss, voltage profile, and voltage stability | IEEE 30-bus and IEEE 118-bus |
| Amit Saraswat and AshishSaini (2013) [22] | HFMOEA | Power loss and voltage stability | IEEE24-busRTS |
| Mojtaba Ghasemi et al. (2014) [23] | HMICA-IWO | Power loss | IEEE 30-bus, IEEE 57-bus and IEEE 118-bus |
| Binod Shaw et al. (2014) [24] | OGSA | Power loss, voltage profile, and voltage stability | IEEE 30-bus, IEEE 57-bus and IEEE 118-bus |
| Abhishek Rajan and T. Malakar (2015) [25] | HFA | Power loss and voltage deviation | IEEE 30-bus and IEEE 118-bus |
| Mojtaba Ghasemi et al. (2015) [26] | MGBTLBO | Power loss | IEEE 14-bus and IEEE30-bus |
| Mehdi Mehdinejad et al. (2016) [27] | ICA-PSO | Power loss and voltage deviation | IEEE57-bus and IEEE 118-bus |
| kuppamuthu sivalingam et al. (2017) [28] | HABC | Power loss | IEEE 6-bus, IEEE14-bus, and IEEE 30-bus |
| Kasem Nuaekaw et al. (2017) [29] | 2ArchMGWO | Power loss and voltage profile | IEEE 30-bus, IEEE 57-bus and IEEE 118-bus |
| Xiaoshun Zhang et al. (2017) [30] | ABO-TRL | Power loss and voltage deviation | IEEE118-bus and IEEE 300-bus |
| Khaled ben oualid Medania (2018) [31] | WOA | Power loss | IEEE 14-bus, IEEE 30-bus, Algerian electric 114-bus |
| SK. Mahammad Shareefa and R. Srinivasa Rao (2018) [32] | ABC-FF | Power loss and voltage stability | IEEE 14 and IEEE 39 bus |
| Hotaka yoshida and Yoshikazu fukuyama (2018) [33] | DEEPSO | Power loss | IEEE 30-bus, IEEE 57-bus and IEEE 118-bus |

Recently, Sine, Cosine Algorithm (SCA) has been a new meta-heuristic search algorithm. It has been proposed by Seyedali Mirjalili in 2016. It has been

described in [34] that the SCA holds a mass of advantages and it is different from the other meta heuristic algorithms like GSA etc. These are shown in

detail in [34]. Moreover, in [34], SCA has been tested on 19 different standard benchmark functions and aircraft design problem compared with other meta heuristic algorithms such as the Firefly Algorithm (FA), Bat Algorithm (BA), Flower Pollination Algorithm (FPA) and Gravitational Search Algorithm (GSA).

It was found that the effects received by SCA in most cases provide superior results and in all cases are comparable with others. The most significant feature of the SCA is that creating multiple initial random candidate solutions and calls for them to fluctuate outwards or towards the best result utilizing a mathematical model based on sine and cosine functions. Several random and adaptive variables also are integrated to this algorithm to emphasize exploration and exploitation of the search space in different milestones of optimization.

For all these grounds, in this paper SCA is chosen in order to solve the ORPD problem in addition with FACTS devices. Two types of FACTS devices, Static Var Compensator (SVC) and Thyristor Controlled Series Capacitor (TCSC) are taken with the conventional ORPD problem. The primary reason for SVC is to absorb or generate reactive power depends upon the requirement of the reactive power in the system to improve the electric potential profile and trim back the system losses. Also, TCSC provides continuous control of active power of the line with variable series capacitance. Along with the conventional variables, the location and sizing as well considered as the variables in the optimization problem. In order to evaluate the proposed algorithm, it was tested on IEEE 14-bus, 57-bus and 118-bus test systems with different objective functions that reflect active power losses and voltage profile improvement, and results obtained from SCA are compared with those reported in the literature.

Power Flow Model for FACTS Devices

FACTS devices are the power electronics based solid state converters that can be integrated in power system as shunt and series connected devices. The series controllers build up voltage in series with the line and the shunt controllers injects current into the system. The combined series and shunt controllers inject both voltage and current into the system. Shunt compensation are used to supply reactive power compensation and series compensator is used to heighten the power flow [35-38]. Two types of FACTS devices, namely static VAR compensators (SVC) and thyristor controlled series capacitors (TCSC) are employed in the transmission network:

- The SVC can be run as either inductive or capacitive compensation. It can be modeled as a fixed condenser and a thyristor-controlled reactor. Thus the part of the SVC is either to inject reactive power to the coach or to absorb reactive power from the bus where it is plugged in.
- TCSC: By modifying the line reactance TCSC acts as either inductive or capacitive compensator. The

maximum value of the capacitance is fixed at $-0.8X_{Line}$ and $0.2X_{Line}$ is the maximum value of the inductance.

A. Modeling of SVC

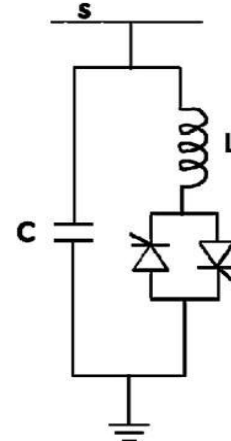


Figure 1: SVC model

The schematic diagram of SVC device is illustrated in Fig. 1. It consists of fixed capacitor and thyristor-controlled reactor. The equivalent susceptance B_{eq} , which neglects harmonic current, can be expressed as

$$B_{eq} = B_L(\alpha) + B_C \tag{1}$$

Where,

$$B_L(\alpha) = -\frac{1}{\omega L} \left(1 - \frac{2\alpha}{\pi}\right) \text{ and } B_C = \omega \times C$$

The SVC is shunt connected static VAR generator or absorber whose output is adjusted to exchange capacitive or inductive current so as to maintain or control specific parameters of electrical power system, typically a bus voltage. The reactive power provided by SVC in the power flow framework can be expressed equally

$$Q_{SVC} = -V_k^2 \times B_{SVC} \tag{2}$$

B. Modeling of TCSC

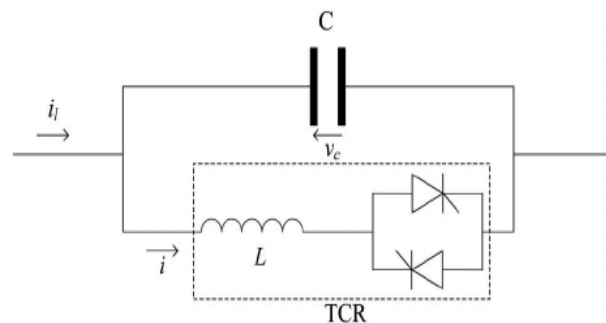


Figure 2: TCSC model

Fig. 2 presents the general circuit structure of TCSC. It consists of a series capacitor in parallel with a thyristor-controlled reactor (TCR). TCR is a variable reactor X_L controlled by firing angle (α). The effective reactance of TCSC may be represented as follows:

$$X_{TCSC}(\alpha) = \frac{X_C X_L(\alpha)}{X_L(\alpha) - X_C} = -jX_C \quad (3)$$

2. Problem Formulation

The solution of the optimal reactive power dispatch (ORPD) problem involves the optimization of the non-linear objective function with non-linear system constraints.

2.1. Minimization of real power losses

The main objective of multi objective optimization is to minimize the active power loss in the transmission network, which is set as follows [8-34]:

$$F_1 = \sum_{k=1}^{NT} P_{loss,k} = \sum_{k=1}^{NT} G_k (V_i^2 + V_j^2) - 2V_i V_j \cos(\delta_i - \delta_j) \quad (4)$$

Where NT is the number of transmission lines, G_k is the conductance of the k^{th} line, V_i and V_j are the voltage magnitude of the i^{th} and j^{th} buses, and δ_i and δ_j are the voltage phase angles of i^{th} and j^{th} buses.

2.2. Improvement of voltage profile

Another objective of this problem is to improve the voltage profile which is formulated mathematically as follows [13,17,19-21,24,29],

$$F_2 = \sum_{i=1}^{NPQ} |V_{i,spec} - V_i| \quad (5)$$

Where NPQ is the number of load buses in the power system and V_i is the reference value of the voltage magnitude of the i^{th} bus which is equal to 1.0 (pu). By combining the Eq.(4) and Eq. (5) leads to the main objective function as follows:

$$F_{obj} = F_1 + F_2 = \left(\sum_{k=1}^{NT} P_{loss,k} \right) + \left(\sum_{i=1}^{NPQ} |V_{i,spec} - V_i| \right) \quad (6)$$

2.3. Constraints

2.3.1. Equality constraints

These constraints, which are load flow equations, are described as follows

$$P_{Gi} - P_{Di} - \sum_{j \in NB} V_i V_j (G_{ij} \cos \delta_{ij} + B_{ij} \sin \delta_{ij}) = 0 \quad (7)$$

$$Q_{Gi} - Q_{Di} - \sum_{j \in NB} V_i V_j (G_{ij} \sin \delta_{ij} + B_{ij} \cos \delta_{ij}) = 0 \quad (8)$$

Where NB is the number of buses, P_{Gi} and Q_{Gi} are generated active and reactive power, P_{Di} and Q_{Di} are load active and reactive power, G_{ij} is the transfer conductance and B_{ij} is the transfer susceptance between i^{th} bus and j^{th} bus, respectively.

2.3.2. Inequality constraints

2.3.2.1. Generator constraints

Generator voltages, reactive outputs ought to be limited by their lower and upper limits as follows

$$Q_{G,i}^{\min} \leq Q_{G,i} \leq Q_{G,i}^{\max} \quad i \in NG \quad (9)$$

$$V_{G,i}^{\min} \leq V_{G,i} \leq V_{G,i}^{\max} \quad i \in NG \quad (10)$$

2.3.2.2. Transformer constraints

Transformer tap setting are bounded as follows:

$$T_i^{\min} \leq T_i \leq T_i^{\max} \quad i \in \text{No.of transformers} \quad (11)$$

2.3.2.3. Shunt VAR compensator constraints

Shunt VAR compensators ought to be restricted by their lower and upper limits as follows

$$Q_{C,i}^{\min} \leq Q_{C,i} \leq Q_{C,i}^{\max} \quad i \in NC \quad (12)$$

2.3.2.4. Security constraints

These include the constraints of voltages at load buses and transmission line loading as follows:

$$V_{L,i}^{\min} \leq V_{L,i} \leq V_{L,i}^{\max} \quad i \in NPQ \quad (13)$$

$$S_{L,i} \leq S_{L,i}^{\max} \quad i \in NT \quad (14)$$

2.3.2.5. SVC constraints

$$Q_{svc(s),\min} \leq Q_{svc(s)} \leq Q_{svc(s),\max} \quad \text{where } (s) \in NSVC \quad (15)$$

Where $Q_{SVC(s)}$ is the VAR rating of SVC and $Q_{SVC(s),\min}$ and $Q_{SVC(s),\max}$ are the minimum and maximum VAR limits of SVC. $NSVC$ is the number of nodes having SVC. (s) represents the current SVC bus number under consideration.

2.3.2.6. TCSC var constraints

$$-0.7 X_{L,TCSC} \leq X_{TCSC(s)} \leq 0.2 X_{L,TCSC} \quad \text{where } (s) \in NTCSC \quad (16)$$

where $X_{L,TCSC}$ is the reactance of the line, where TCSC is connected. $X_{TCSC(s)}$ is the reactance of the s^{th} TCSC. $NTCSC$ is the number of lines having TCSC. (s) represents the current TCSC line number under consideration.

Eq. (4) and Eq. (5) are changed to the following form using penalty terms to the objective function:

$$F_{new} = F_{obj} + \lambda_v \sum_{i=1}^{NPQ} (V_i - V_i^{\lim})^2 + \lambda_Q \sum_{i=1}^{NG} (Q_{G,i} - Q_{G,i}^{\lim})^2 \quad (17)$$

x^{\lim} is the limit value of the dependent variable $x = (V_i \text{ and } Q_{G,i})$ and given as:

$$x^{\lim} = x^{\max} \quad \text{if } x > x^{\max}, \text{ and } x^{\lim} = x^{\min} \quad \text{if } x < x^{\min}$$

Where λ_v and λ_Q are the weighting factors to enhance the objective function.

Sine Cosine Optimization Algorithm

Regardless of the differences between algorithms in the field of stochastic population-based optimization, the green is the divergence of the optimization process into two phases: exploration versus exploitation. In the former phase, an optimization algorithm combines the random solutions in the set of solutions abruptly with a high rate of randomness to find the shining parts of the search space. In the development phase, all the same, there are gradual changes in the random solutions, and random variations are considerably less than those in the exploration stage.

In this SCA [35], the following position updating equations is proposed for both phases:

$$X_i^{t+1} = X_i^t + r_1 \times \sin(r_2) \times \|r_3 P_i^t - X_i^t\| \quad (18)$$

$$X_i^{t+1} = X_i^t + r_1 \times \cos(r_2) \times \|r_3 P_i^t - X_i^t\| \quad (19)$$

where X_i^t is the position of the current solution in i^{th} dimension at t^{th} iteration, $r_1/r_2/r_3$ are random numbers, P_i is position of the destination point in i^{th} dimension, and $\|$ indicates the absolute value.

By combining the Eq. (18) and Eq. (19), it will be used as,

$$X_i^{t+1} = \begin{cases} X_i^t + r_1 \times \sin(r_2) \times \|r_3 P_i^t - X_i^t\| r_4 < 0.5 \\ X_i^t + r_1 \times \cos(r_2) \times \|r_3 P_i^t - X_i^t\| r_4 \geq 0.5 \end{cases} \quad (20)$$

where r_4 is a random number in $[0,1]$.

From the Eq. (18), there are four main parameters in the SCA: r_1, r_2, r_3 and r_4 .

- The parameter r_1 dictates the next position's region (or motion direction) which could be either in the space between the solution and destination or outside it.
- The parameter r_2 defines how far the trend should be towards or outwards the destination.
- The parameter r_3 brings a random weight for the destination in order to stochastically emphasize ($r_3 > 1$) or deem- phases ($r_3 < 1$) the effect of destination in defining the space.
- Lastly, the parameter r_4 equally switches between the sin and cosine components in Eq. (17).

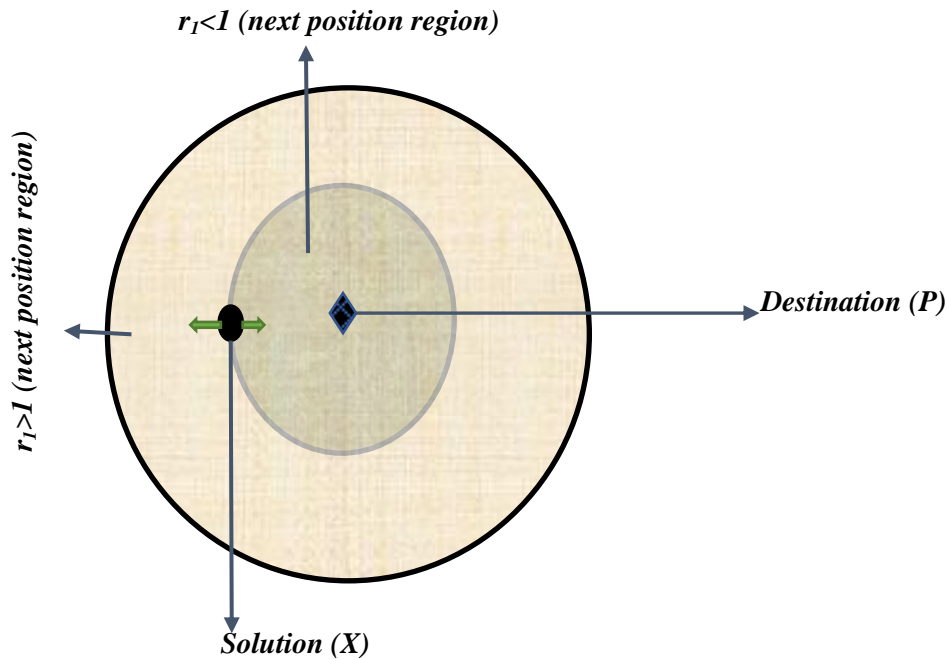


Figure 3: Properties of Sine and Cosine on the side by side post

The effects of Sine and Cosine on Eqs. (18) and(19) are illustrated in Fig. 3. This number shows that how the proposed equations define, a space between two solutions in the search blank. It should be noted that this equivalence can be stretched to higher dimensions, although a two-dimensional example is illustrated in Fig. 3. The cyclic pattern of sin and cosine function allows a solution to be re-positioned around another solution. This can guarantee exploitation of the space defined between two solutions. For researching the search space, the solutions should be capable to seek outside the space between their corresponding destinations as well. This

can be achieved by changing the sphere of the sin and cosine functions. A conceptual model of the effects of the sine and cosine functions with the range in $[-2, 2]$ is illustrated in the Fig. 4. This copy establishes how fluctuating the range of sine and cosine functions requires a solution to update its position out of entries or in the space between itself and another solution. The random location either at the rear or outside is achieved by assigning a random number for r_2 in $[0, 2\pi]$ in Eq. (20). Therefore, this mechanism guarantees exploration and exploitation of the search space respectively.

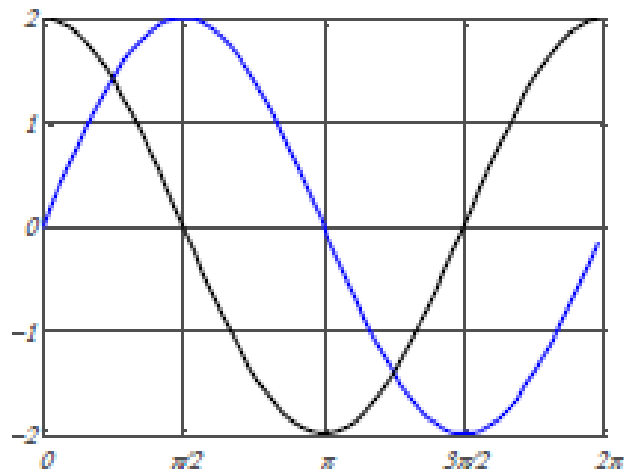


Figure 4: Sine and cosine with range of [-2,2]

The following equation is used to update the value of r_i in Eqs. (15) to (17),

$$r_1 = a - t \frac{a}{T} \quad (18)$$

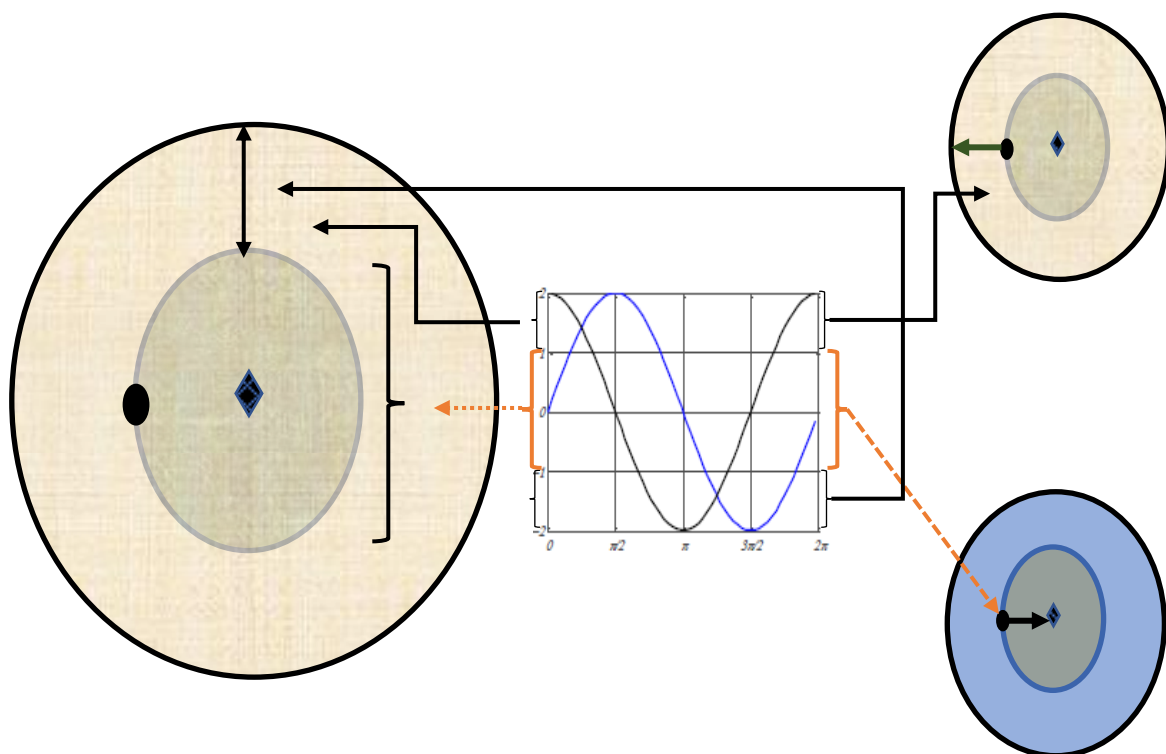


Figure 5: Sine and cosine with the range in [-2,2] allow a solution to go around (inside the space between them) or beyond (outside the space between them) the destination

Where t is the current iteration, T is the maximum number of iterations, and a is a constant.

From the explanation, equation decreases the range of sine and cosine functions over the course of iterations are shown in Fig. 5.

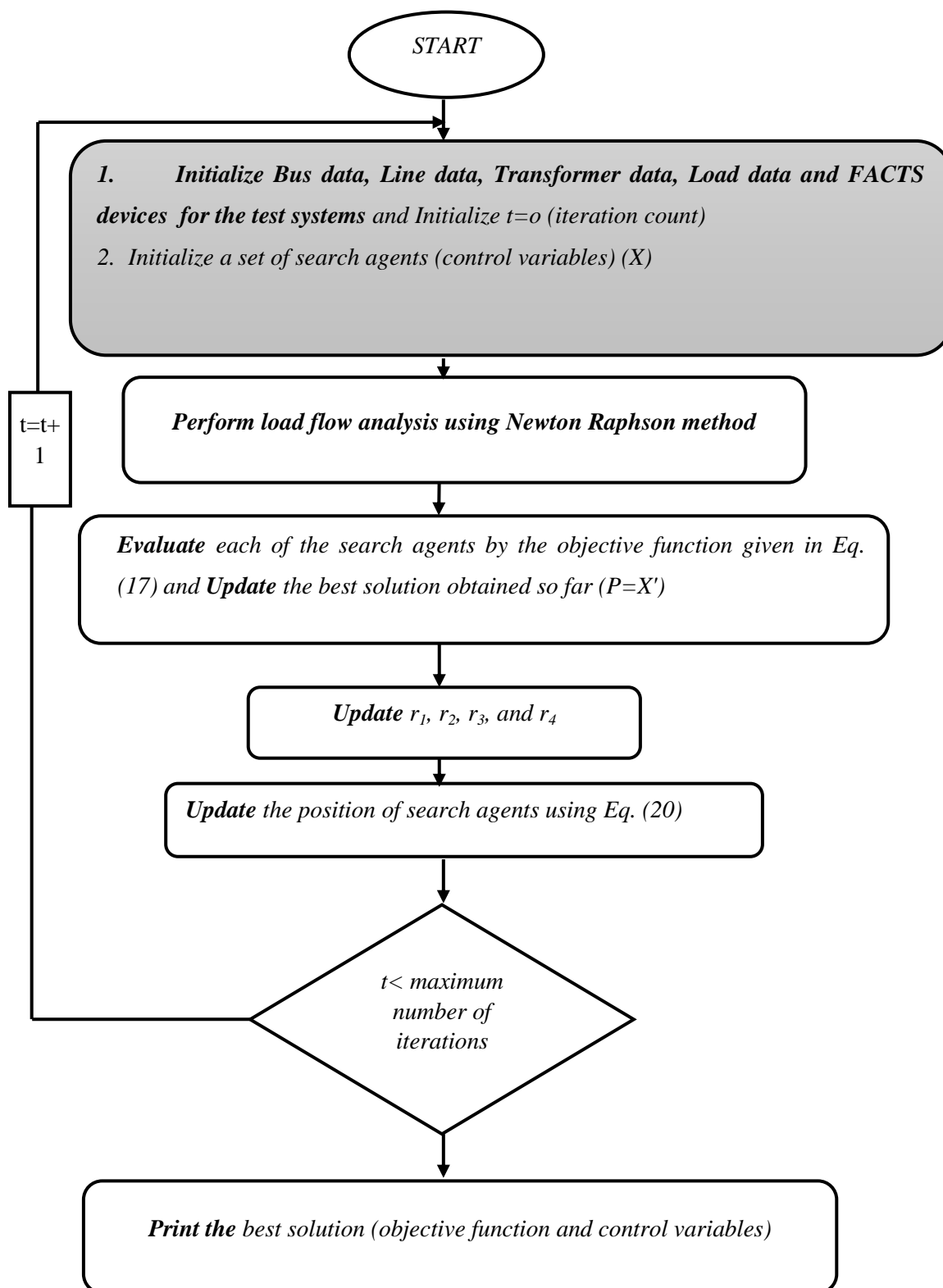


Figure 6: Flowchart for the solution of the SCA Algorithm for ORPD problem

2.4. Implementation of Sine Cosine Optimization Algorithm for ORPD with FACTS devices

Step1: Initialization the set of search agents (control variables) (X).

$$X^T = [V_{G1} \dots V_{GNPV}, Q_{C1} \dots Q_{CNC}, T_1 \dots T_{NT}, Q_{svc(1)} \dots Q_{svc(NSVC)}, X_{TCSC(1)} \dots X_{TCSC(NTCSC)}]$$

Step 2: Perform Newton Raphson load flow analysis, and ascertain the solution using Eq. (17) for the initialized set of search agents from step 1.

Step 3: Save the best solutions obtained so far, assigns it as the last point (P=X'), and update the other solutions with respect to it.

Step 4: Meanwhile, the ranges of sine and cosine functions ($r_1, r_2, r_3,$ and r_4) are updated to emphasize development of the search space as the iteration counter increases

Step 5: Check the termination criteria (In this study, SCA algorithm terminates the optimization process when the iteration counter goes higher than the upper limit number

of iterations by default). If it is satisfied, publish the best solution (objective function and control variables) else Update the position of search agents using Eq. (20) and go to step 2.

Test Systems

In this paper, sine cosine algorithm is applied to standard IEEE 14, IEEE 57 and IEEE 118 test systems for the solution of the conventional ORPD problem. 25 Trial runs were also taken for each of the process and the best results of each process are presented for comparison. The maximum number of iterations was taken 1000, for each case. Single line diagram of all the test systems were given in Fig. 7, 8 and Fig. 9 with its description is depicted in Table 2. Simulations are carried out using *Matlab* R2015a software [39]. All the necessary details about the test systems were taken from MATPOWER tool box [40].

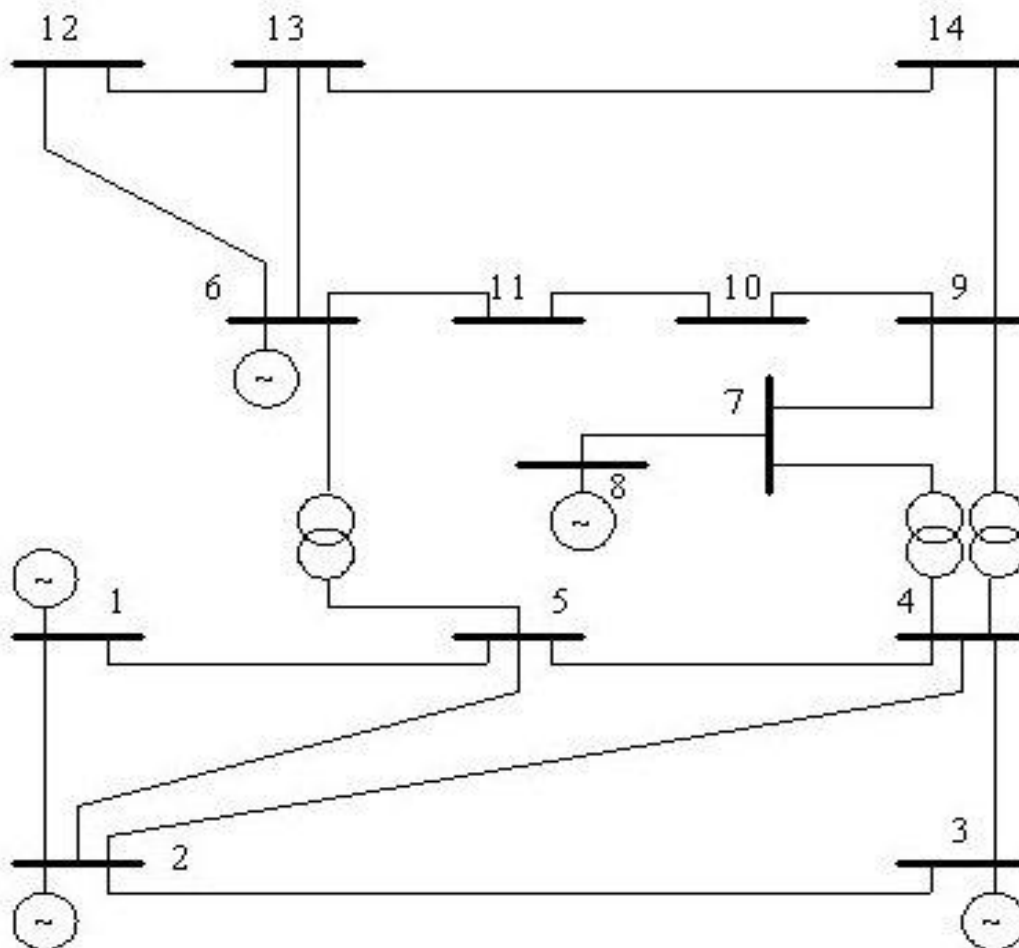


Figure7: Single line diagram of IEEE-14 bus system

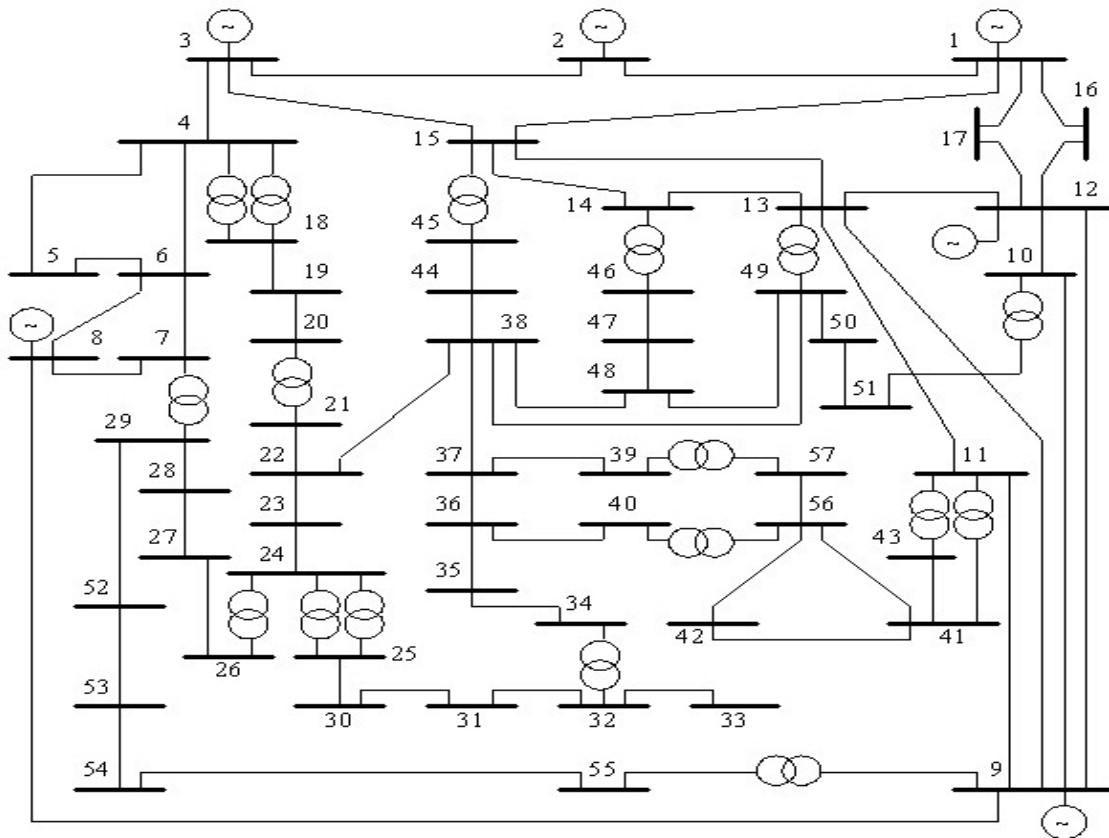


Figure 8: Single line diagram of IEEE-57 bus system

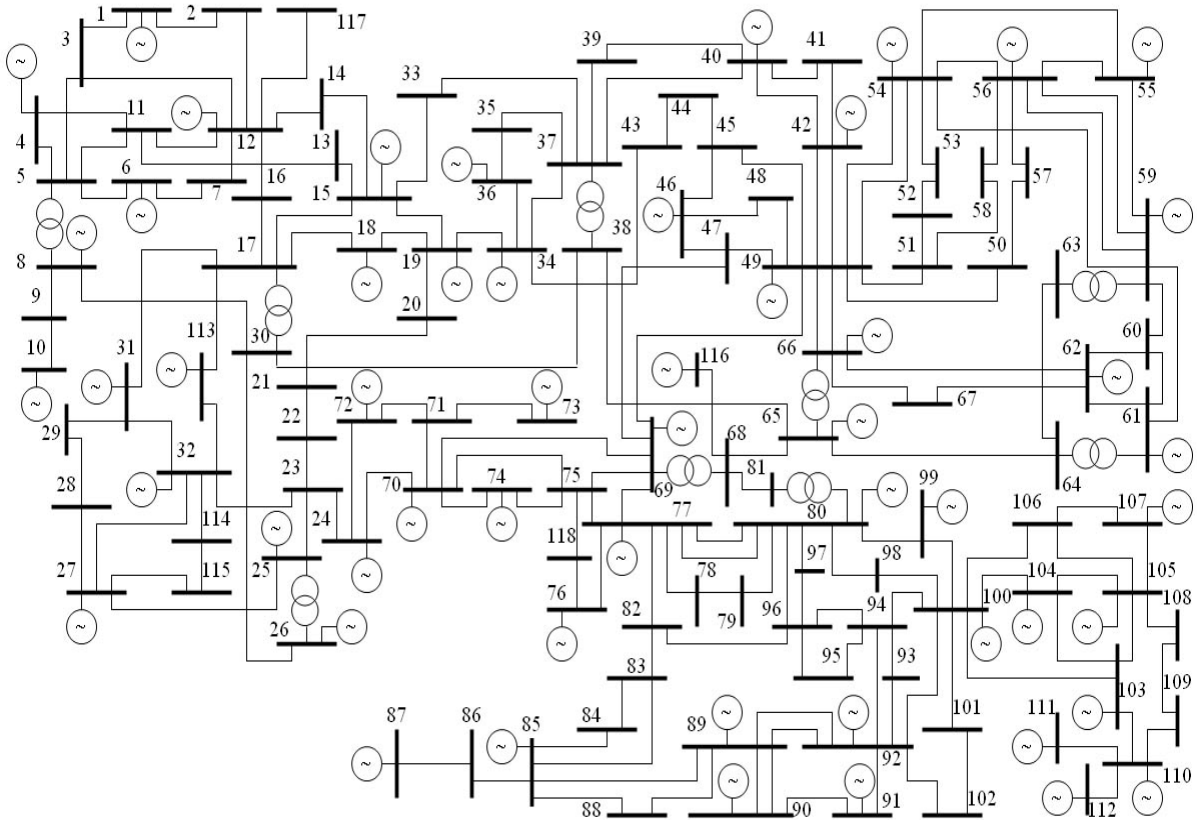


Figure 9: Single line diagram of IEEE-118 bus system

Table 2: Description of test systems – Base case

| Description | IEEE 14-bus | IEEE 57-bus | IEEE 118-bus |
|-----------------------------|-------------|-------------|--------------|
| Buses | 14 | 57 | 118 |
| Generators | 5 | 7 | 54 |
| Transformers | 3 | 15 | 9 |
| Shunts | 2 | 3 | 14 |
| Branches | 20 | 80 | 186 |
| Control variables | 10 | 25 | 77 |
| Base case P_{Load} (MW) | 259.00 | 1250.80 | 4242 |
| Base case Q_{Load} (MVar) | 73.50 | 336.40 | 1438 |
| Base case P_{Loss} (MW) | 13.49 | 28.462 | 132.283 |

Results and Discussion

2.5. Test system 1: Standard IEEE-14 bus system

The standard IEEE 14-bus system consists of 20 transmission lines, five generators at 1, 2, 3, 6 and 8 and 15 branches under load tap setting transformer branches for 4-7, 4-9 and 5-6. The reactive power sources are

considered at buses 9 and 14. The system line data, bus information, variable limits and the initial values of the control variables were presented in [40]. Initially, P_{Load} is 259 MW and Q_{Load} is 73.50 MVar before optimization. The upper and lower limits of generation reactive power and control variable limits of test system are given in Table 3, respectively.

Table 3: Limits of control variables for IEEE 14 bus system

| Generator | | Transformer | | Reactive power sources | | SVC | | TCSC | |
|-------------|-------------|-------------|-------------|------------------------|-------------|-----------------|-----------------|------------------|------------------|
| V_G^{min} | V_G^{max} | T_i^{min} | T_i^{max} | Q_C^{min} | Q_C^{max} | Q_{SVC}^{min} | Q_{SVC}^{max} | X_{TCSC}^{min} | X_{TCSC}^{max} |
| 0.95 | 1.1 | 0.9 | 1.1 | -0.3 | 0.0 | -0.3 | 0.3 | $-0.8X_{ij}$ | $0.2X_{ij}$ |

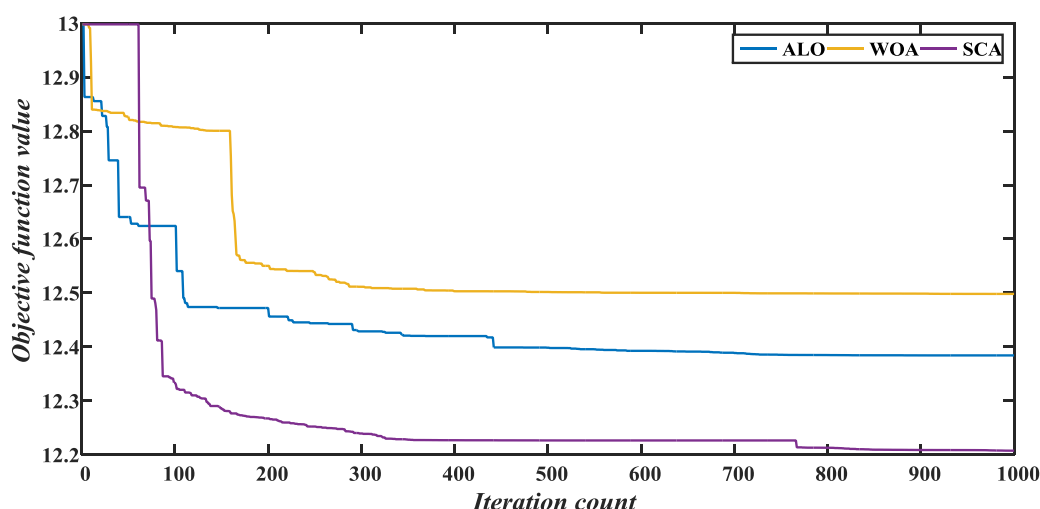


Figure10:Convergence characteristics of IEEE-14 bus system

The proposed approach is applied for minimisation of active power losses with improvement of voltage profile as the objective function. The obtained optimal values of control variables from the proposed SCA method are presented in Table 4. The obtained minimum real power loss from the proposed SCA approach is 11.9391 MW from the basecase real power loss of 13.49 MW. Fig. 10 shows the convergence characteristic of SCA for the proposed objective function. It shows that

the SCA finds the better convergence compared with WOA and ALO. The results obtained from the proposed GSA method were compared with the other methods in the literature with the computational time of each algorithm are given in Table 5. It can be assured that both the power loss and the computing time of SCA is less than the other evolutionary algorithms reported in the literature.

Table 4: Best control variables settings and active power loss for IEEE 14 bus system

| Optimization method | SCA (proposed) | WOA (proposed) | ALO (proposed) | HSA [35] | IHSA [35] |
|---------------------|----------------|----------------|----------------|---------------|---------------|
| V_1 (pu) | 1.0931 | 0.9760 | 1.0515 | 1.099 | 1.1 |
| V_2 (pu) | 1.0116 | 1.0232 | 0.9930 | 1.074 | 1.0931 |
| V_3 (pu) | 1.1000 | 1.0235 | 1.0177 | 1.0587 | 1.0687 |
| V_6 (pu) | 1.0865 | 1.1000 | 1.1000 | 1.0938 | 1.0954 |
| V_8 (pu) | 1.0580 | 1.0866 | 1.0753 | 1.0767 | 1.0865 |
| T_{4-7} | 1.0931 | 1.0589 | 1.0575 | 0.9916 | 0.97347 |
| T_{4-9} | 1.0972 | 1.1000 | 1.0472 | 0.9872 | 1.007 |
| T_{5-6} | 1.0594 | 1.0354 | 0.9763 | 0.9864 | 1.0526 |
| Q_{c-9} (MVar) | 27.3476 | 25.5553 | 29.6613 | 25.105 | 28.315 |
| Q_{c-14} (MVar) | 29.2124 | 25.9727 | 25.3325 | 6.1897 | 2.9778 |
| Q_{svc} (MVar) | (12) 6.6162 | (3) 7.4779 | (3) 20.1292 | (4)10.561 | (6)25.883 |
| Q_{svc} (MVar) | (14) 4.1548 | (1) 4.2637 | (8) 19.728 | | |
| Q_{svc} (MVar) | (5) 29.2592 | (5) 27.7675 | (14) 22.793 | | |
| X_{TCSC} (pu) | 0.02791(2-3) | 0.81514 (3-4) | 0.02134(2-3) | 0.05148 (2-3) | 0.39109 (3-4) |
| X_{TCSC} (pu) | 0.04112(3-4) | 0.05125 (7-9) | 0.54321(12-6) | | |
| X_{TCSC} (pu) | 0.0132(12-6) | 0.05327(10-11) | 0.76543(7-9) | | |
| P_{Loss} (MW) | 11.9391 | 12.2801 | 12.4312 | 12.198 | 12.065 |

Table 5: Best solutions of all algorithms for IEEE 14 bus system

| Algorithms | Best (pu) | Worst (pu) | Mean (pu) | Std. deviation | % P_{save} |
|----------------------|---------------|----------------|---------------|---|--------------|
| DE [10] | 0.1324 | 0.1328 | 0.1325 | 1.61×10^{-4} | 1.86 |
| PSO [34] | 0.1325 | 0.1340 | 0.1335 | 0.64×10^{-3} | 1.75 |
| ACOR[34] | 0.1312 | 0.1357 | 0.1339 | 7.1854×10^{-2} | 2.72 |
| DE/best/2/bin[34] | 0.1299 | 0.1301 | 0.1309 | 6.5036×10^{-4} | 3.7 |
| ABC[34] | 0.1293 | 0.1312 | 0.1296 | 9.422×10^{-4} | 4.13 |
| LCA[34] | 0.1299 | 0.1316 | 0.1305 | 5.5283×10^{-3} | 3.71 |
| CSS[34] | 0.1297 | 0.1330 | 0.1312 | 4.206×10^{-2} | 3.82 |
| BRCFF[34] | 0.1293 | 0.1298 | 0.1293 | 8.8191×10^{-5} | 4.18 |
| BB-BC[34] | 0.1300 | 0.1323 | 0.1311 | 4.7604×10^{-3} | 3.6 |
| PBIL[34] | 0.1300 | 0.1319 | 0.1309 | 9.7075×10^{-4} | 3.63 |
| TLA[34] | 0.1292 | 0.1295 | 0.1293 | 9.0283×10^{-5} | 4.2 |
| MTLA [34] | 0.1291 | 0.1292 | 0.1292 | 7.6832×10^{-5} | 4.3 |
| DDE [34] | 0.1293 | 0.1293 | 0.1293 | 5.0065×10^{-5} | 4.16 |
| MTLA-DDE[34] | 0.1290 | 0.1290 | 0.1290 | 6.486×10^{-6} | 4.39 |
| TLBO [26] | 0.1299 | 0.1299 | 0.1299 | 9.28×10^{-5} | 3.72 |
| BBPSO [26] | 0.1299 | 0.1300 | 0.1299 | 9.45×10^{-5} | 3.69 |
| BBDE [26] | 0.1300 | 0.1311 | 0.1300 | 8.62×10^{-5} | 3.64 |
| GBTLBO [26] | 0.1242 | 0.1242 | 0.1242 | 0.75×10^{-5} | 7.97 |
| MGBTLBO [26] | 0.1231 | 0.1236 | 0.1232 | 0.42×10^{-5} | 8.74 |
| HSA [35] | 0.1281 | 0.1283 | 0.1281 | 5.346×10^{-6} | 5.07 |
| IHSA [35] | 0.1279 | 0.1288 | 0.1281 | 6.974×10^{-6} | 5.20 |
| HSA [35] with facts | 0.12198 | 0.12243 | 0.1222 | 6.73×10^{-6} | 9.58 |
| IHSA [35] with facts | 0.12065 | 0.12111 | 0.12091 | 6.81×10^{-6} | 10.56 |
| ALO (proposed) | 0.1243 | 0.1257 | 0.1261 | 5.95×10^{-6} | 7.85 |
| WOA (proposed) | 0.1228 | 0.1284 | 0.1279 | 5.79×10^{-6} | 8.96 |
| SCA (proposed) | 0.1193 | 0.11982 | 0.1196 | 4.73×10^{-6} | 11.56 |

2.6. Test system 2: Standard IEEE-57 bus system

The standard IEEE 57-bus system consists of 80 transmission lines, seven generators at 1, 2, 3, 6, 8, 9, 12 and branches under load tap setting transformer branches. The reactive power sources are viewed as buses 18, 25 and 53. The system line data, bus information, variable

limits and the initial values of the control variables were presented in [12,17,19,23,24]. The search space of this case system has 31 dimensions, including 7 generator voltages, 15 transformer taps and 3 reactive power sources with three SCR and TCSCs (location and sizing). The upper and lower boundaries of generation reactive

power and control variable limits of trial system are given in Table 6. The entire system load is 1250.8 MW and 336.4 MVar. The initial system active power loss is 28.462 MW.

Table 6:Limits of control variables for IEEE-57 bus system

| Reactive power sources (pu) | | | | | | | | | | | | | | |
|------------------------------------|-------------|-------|-----------------|-------|------|-------|-------------------------|-------------|-----|------------------|------|-----|------|------|
| Bus No | Q_C^{min} | | | | | | | Q_C^{max} | | | | | | |
| | 1 | 2 | 3 | 6 | 8 | 9 | 12 | 1 | 2 | 3 | 6 | 8 | 9 | 12 |
| Values | -1.4 | -0.17 | -0.1 | -0.08 | -1.4 | -0.03 | -1.5 | 2.0 | 0.5 | 0.6 | 0.25 | 2.0 | 0.09 | 1.55 |
| Generator voltages (pu) | | | | | | | Transformer taps | | | | | | | |
| V_G^{min} | | | V_G^{max} | | | | T_i^{min} | | | T_i^{max} | | | | |
| 0.95 | | | 1.1 | | | | 0.9 | | | 1.1 | | | | |
| SVC variables (pu) | | | | | | | TCSC (pu) | | | | | | | |
| Q_{svc}^{min} | | | Q_{svc}^{max} | | | | X_{TCSC}^{min} | | | X_{TCSC}^{max} | | | | |
| -0.3 | | | 0.3 | | | | -0.8 X_{ij} | | | 0.2 X_{ij} | | | | |

Table 7:Best control variables settings and active power loss for IEEE 57 bus system

| Control variables | SCA (proposed) | WOA (proposed) | ALO (proposed) | HSA [36] | IHSA[36] |
|-------------------|----------------|-----------------|-----------------|-----------------|---------------|
| V_1 (pu) | 1.1000 | 1.1000 | 1.1000 | 1.0959 | 1.0951 |
| V_2 (pu) | 1.1000 | 1.1000 | 1.0986 | 1.0823 | 1.0876 |
| V_3 (pu) | 1.0768 | 1.1000 | 1.0865 | 1.0615 | 1.0730 |
| V_6 (pu) | 1.0558 | 1.1000 | 1.0789 | 1.0791 | 1.0768 |
| V_8 (pu) | 1.0566 | 1.1000 | 1.1000 | 1.0956 | 1.0978 |
| V_9 (pu) | 1.0795 | 1.1000 | 1.0865 | 1.0615 | 1.0687 |
| V_{12} (pu) | 1.1000 | 1.1000 | 1.0826 | 1.0543 | 1.0524 |
| T_{4-18} | 0.9037 | 0.9000 | 1.0983 | 1.0868 | 1.0914 |
| T_{4-18} | 1.0765 | 1.1000 | 1.0996 | 1.0431 | 1.0533 |
| T_{21-20} | 1.0284 | 1.1000 | 1.0822 | 1.0516 | 1.0374 |
| T_{24-26} | 0.9033 | 0.9000 | 1.0274 | 1.0448 | 1.0383 |
| T_{7-29} | 0.9998 | 0.9000 | 1.0593 | 1.0312 | 0.9993 |
| T_{34-32} | 0.9000 | 1.1000 | 1.0299 | 1.0654 | 1.0485 |
| T_{11-41} | 0.9637 | 0.9658 | 1.0757 | 0.972 | 0.96148 |
| T_{15-45} | 1.0515 | 0.9868 | 0.9911 | 0.97004 | 0.96166 |
| T_{14-46} | 1.0075 | 0.9075 | 1.0160 | 0.95267 | 0.94767 |
| T_{10-51} | 1.0257 | 0.9868 | 1.0395 | 0.98042 | 0.98225 |
| T_{13-49} | 1.0141 | 0.9000 | 0.9920 | 0.9645 | 0.93838 |
| T_{11-43} | 1.0432 | 0.9435 | 1.0431 | 1.0854 | 1.0779 |
| T_{40-56} | 0.9143 | 1.0554 | 0.9963 | 0.95482 | 0.9646 |
| T_{39-57} | 0.9753 | 1.0320 | 1.0450 | 1.0534 | 1.0720 |
| T_{9-55} | 0.9699 | 0.9410 | 1.0491 | 1.0224 | 1.0016 |
| Q_{C-18} (MVar) | 11.3872 | 12.5971 | 13.0281 | 15.027 | 17.2000 |
| Q_{C-25} (MVar) | 11.2767 | 10 | 24.602 | 2.2793 | 5.0562 |
| Q_{C-53} (MVar) | 11.7701 | 20.3131 | 13.4127 | 15.376 | 16.1050 |
| Q_{svc} (MVar) | 24.4867 (13) | 24.7657 (2) | 22.7575(45) | 13.715(41) | 25.5950 (37) |
| Q_{svc} (MVar) | 29.0054 (2) | 11.8676(21) | 23.6767(37) | 10.717(33) | 12.1650(13) |
| Q_{svc} (MVar) | 5.77056 (4) | 4.76767(41) | 10.77056 (13) | 14.337 (45) | 20.7940 (7) |
| X_{TCSC} (pu) | 0.013891(2-3) | -0.12133(9-11) | 0.12344(2-3) | 0.26322 (54-55) | -0.0332(9-11) |
| X_{TCSC} (pu) | 0.016119(8-9) | 0.175543(36-40) | -0.12878(50-51) | | |
| X_{TCSC} (pu) | 0.01767(9-12) | 0.176757(54-55) | 0.044322(2-3) | 0.13096 (50-51) | 0.1166 (9-12) |
| P_{Loss} (MW) | 21.7272 | 23.0555 | 23.7039 | 22.504 | 22.057 |

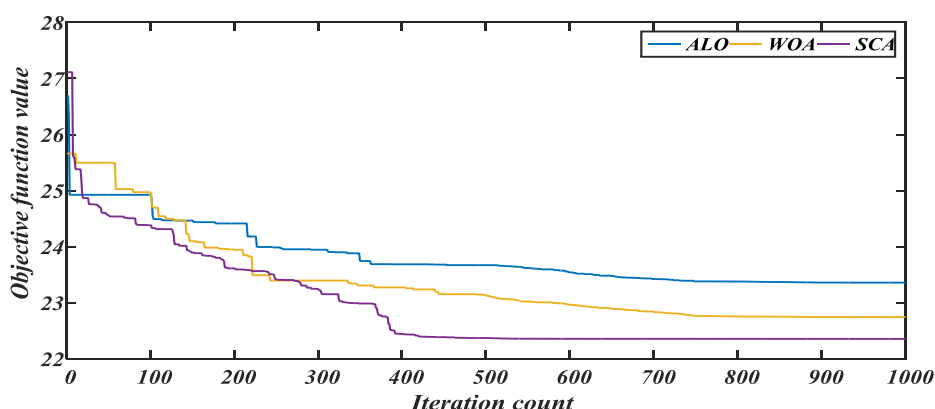


Figure11:Convergence characteristics of IEEE-57 bus system

Table 8: Best solutions of all algorithms for IEEE 57 bus system.

| Algorithms | Best (pu) | Worst (pu) | Mean (pu) | Std.Deviation | % P_{Save} |
|-----------------------|----------------|----------------|----------------|--|--------------|
| NLP [16] | 0.25902 | 0.30854 | 0.27858 | 1.167×10^{-2} | 8.9934 |
| CGA [16] | 0.25244 | 0.27508 | 0.26294 | 6.295×10^{-3} | 11.3059 |
| AGA [16] | 0.24565 | 0.26762 | 0.25128 | 6.006×10^{-3} | 13.6925 |
| PSO-w [16] | 0.24271 | 0.26153 | 0.24726 | 7.014×10^{-3} | 14.7266 |
| PSO-cf[16] | 0.24280 | 0.26033 | 0.24698 | 6.629×10^{-3} | 14.6925 |
| CLPSO [16] | 0.24515 | 0.24781 | 0.24673 | 9.341×10^{-4} | 13.8669 |
| SPSO-07[16] | 0.24430 | 0.25457 | 0.24752 | 2.833×10^{-3} | 14.6925 |
| L-DE [16] | 0.27813 | 0.41909 | 0.33178 | 4.707×10^{-2} | 13.8669 |
| L-SACP-DE [16] | 0.27916 | 0.36979 | 0.31033 | 3.223×10^{-2} | 14.1647 |
| L-SaDE[16] | 0.24267 | 0.24391 | 0.24311 | 4.815×10^{-4} | 14.2815 |
| SOA [16] | 0.24265 | 0.24280 | 0.24271 | 4.208×10^{-5} | 14.7443 |
| HSA [17] | 0.24906 | 0.26965 | 0.25924 | - | - |
| HSA [36] | 0.23710 | 0.24272 | 0.23898 | 4.469×10^{-5} | 16.6959 |
| IHSA [36] | 0.23448 | 0.24011 | 0.23755 | 4.177×10^{-5} | 17.6165 |
| HSA [36] with facts | 0.22504 | 0.22534 | 0.22113 | 5.177×10^{-5} | 20.93 |
| IHSA [36] with facts | 0.22057 | 0.22098 | 0.22062 | 5.007×10^{-5} | 22.50 |
| ALO (proposed) | 0.23703 | 0.23855 | 0.23786 | 4.567×10^{-5} | 16.66 |
| WOA (proposed) | 0.23055 | 0.23555 | 0.23455 | 4.877×10^{-5} | 18.88 |
| SCA (proposed) | 0.21727 | 0.21787 | 0.21755 | 4.054×10^{-5} | 23.66 |

Table 8 depicts the solution result for minimization of objective while the best reactive power dispatch solutions for this objective are tabulated. In Table 8, SCA based results are compared to other optimization technique recently reported in the literature like HSA [36] and IHSA [36]. Also, SCA results are compared with newest optimization techniques of ALO and WOA.

In [19], base case power loss for this test power network is reported as 28.462 MW. The percentage save of power loss demonstrates that a power loss reduction of 23.66% (from 28.462 MW to 21.727 MW) is accomplished by using the proposed SCA approach, which is the highest reduction of power loss than that obtained by the other approaches in the literature. Comparative ALO, WOA and SCA based convergence profiles of objective function for this test power system is presented in Fig. 11. From this figure it may be observed

that the convergence profile for the proposed SCA based approach for this test system is capable one.

2.7. Test system 3: Standard IEEE-118 bus system

To test the proposed technique in solving larger power systems, a standard IEEE 118-bus test system is considered. The search space of this case system has 83 dimensions, that is, the 54 generator buses, 64 load buses, 186 transmission lines, 9 transformer taps and 14 reactive power sources addition with 3 SCRs and 3 TCSCs. The system line data, bus data, variable limits and the initial values of control variables were given in [19,23,25, 29]. The maximum and minimum limits of reactive power sources, voltage and tap-setting limits are given in Tables 9 respectively. The system loads are given as follows $P_{load} = 4242$ MW, $Q_{load} = 1438$ MVar. The total power losses are as $P_{loss}=132.283$ MW.

Table 9:Limits of control variables for IEEE-118 bus system

| Reactive power sources (MVA _r) | | | | | | | | | | | | | | | |
|--|-----|----|-----|-----------------|-----|-----|-----------------|-----------------|----|----|----|-----------------|-----|-----|--|
| Q_G^{min} | | | | | | | | Q_G^{max} | | | | | | | |
| Bus No | 5 | 34 | 37 | 44 | 45 | 46 | 48 | 5 | 34 | 37 | 44 | 45 | 46 | 48 | |
| Values | -40 | 0 | -25 | 0 | 0 | 0 | 0 | 0 | 14 | 0 | 10 | 10 | 10 | 15 | |
| Bus No | 74 | 79 | 82 | 83 | 105 | 107 | 110 | 74 | 79 | 82 | 83 | 105 | 107 | 110 | |
| Values | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 12 | 20 | 20 | 10 | 20 | 6 | 6 | |
| Generator voltages (pu) | | | | | | | Transformer tap | | | | | | | | |
| V_G^{min} | | | | V_G^{max} | | | | T_i^{min} | | | | T_i^{max} | | | |
| 0.95 | | | | 1.1 | | | | 0.9 | | | | 1.1 | | | |
| SVC variables (pu) | | | | | | | TCSC (pu) | | | | | | | | |
| Q_{svc}^{min} | | | | Q_{svc}^{max} | | | | Q_{svc}^{min} | | | | Q_{svc}^{max} | | | |
| -0.3 | | | | 0.3 | | | | -0.3 | | | | 0.3 | | | |

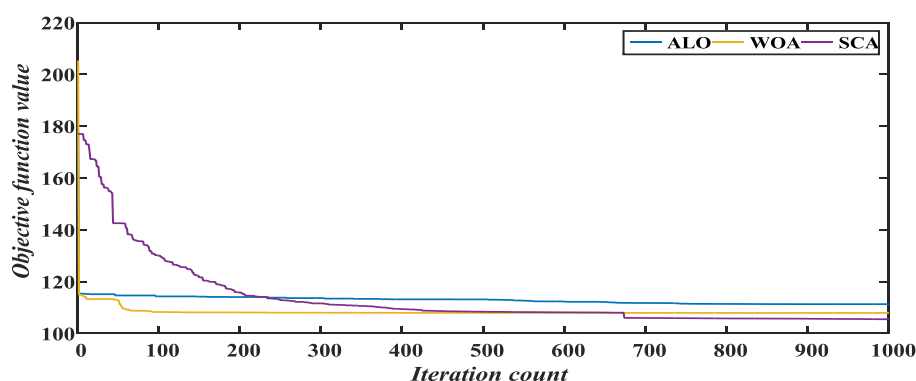


Figure 12:Convergence characteristics of IEEE-118 bus system

Table 10:Best control variables settings and active power loss for IEEE-118 bus system

| Control variables | With FACTS devices | | | Conventional ORPD alone | | | | | |
|----------------------|--------------------|----------------|----------------|-------------------------|----------|---------------|----------|---------|-----------|
| | SCA (proposed) | WOA (proposed) | ALO (proposed) | ICA [23] | IWO [23] | MICA-IWO [23] | GSA [19] | PSO[19] | CLPSO[19] |
| V ₁ (pu) | 1.082472 | 1.087637 | 1.048895 | 1.0080 | 0.9978 | 1.0419 | 0.9600 | 1.0853 | 1.0332 |
| V ₄ (pu) | 1.083338 | 1.087637 | 1.049046 | 1.0296 | 1.0378 | 1.0600 | 0.9620 | 1.0420 | 1.0550 |
| V ₆ (pu) | 1.080483 | 1.085874 | 1.048895 | 1.0149 | 1.0189 | 1.0542 | 0.9729 | 1.0805 | 0.9754 |
| V ₈ (pu) | 1.07779 | 1.087637 | 1.04902 | 1.0381 | 0.9922 | 1.0582 | 1.0570 | 0.9683 | 0.9669 |
| V ₁₀ (pu) | 1.076733 | 1.086423 | 1.049895 | 1.0600 | 1.0245 | 1.0600 | 1.0885 | 1.0756 | 0.9811 |
| V ₁₂ (pu) | 1.078168 | 1.087637 | 1.049544 | 1.0131 | 1.0087 | 1.0511 | 0.9630 | 1.0225 | 1.0092 |
| V ₁₅ (pu) | 1.081264 | 1.087637 | 1.049418 | 1.0006 | 0.9804 | 1.0498 | 1.0127 | 1.0786 | 0.9787 |
| V ₁₈ (pu) | 1.081803 | 1.085983 | 1.049552 | 0.9987 | 0.9883 | 1.0525 | 1.0069 | 1.0498 | 1.0799 |
| V ₁₉ (pu) | 1.082496 | 1.087637 | 1.049648 | 1.0036 | 0.9862 | 1.0490 | 1.0003 | 1.0776 | 1.0805 |
| V ₂₄ (pu) | 1.077607 | 1.087637 | 1.048988 | 1.0388 | 0.9673 | 1.0528 | 1.0105 | 1.0827 | 1.0286 |
| V ₂₅ (pu) | 1.073081 | 1.087637 | 1.048895 | 1.0600 | 1.0515 | 1.0600 | 1.0102 | 0.9564 | 1.0307 |
| V ₂₆ (pu) | 1.083363 | 1.087637 | 1.049297 | 1.0600 | 0.9948 | 1.0600 | 1.0401 | 1.0809 | 0.9877 |
| V ₂₇ (pu) | 1.081682 | 1.087637 | 1.048895 | 1.0093 | 0.9829 | 1.0466 | 0.9809 | 1.0874 | 1.0157 |
| V ₃₁ (pu) | 1.08228 | 1.087637 | 1.048895 | 0.9958 | 0.9461 | 1.0430 | 0.9500 | 0.9608 | 0.9615 |
| V ₃₂ (pu) | 1.08213 | 1.085809 | 1.049384 | 1.0016 | 0.9532 | 1.0453 | 0.9552 | 1.1000 | 0.9851 |
| V ₃₄ (pu) | 1.083463 | 1.087637 | 1.049691 | 1.0267 | 1.0099 | 1.0600 | 0.9910 | 0.9611 | 1.0157 |
| V ₃₆ (pu) | 1.0837 | 1.087637 | 1.04975 | 1.0257 | 1.0019 | 1.0584 | 1.0091 | 1.0367 | 1.0849 |
| V ₄₀ (pu) | 1.080107 | 1.087637 | 1.048895 | 1.0181 | 0.9886 | 1.0384 | 0.9505 | 1.0914 | 0.9830 |
| V ₄₂ (pu) | 1.081575 | 1.087637 | 1.049483 | 1.0285 | 0.9559 | 1.0398 | 0.9500 | 0.9701 | 1.0516 |
| V ₄₆ (pu) | 1.084271 | 1.087637 | 1.048895 | 1.0409 | 1.0205 | 1.0470 | 0.9814 | 1.0390 | 0.9754 |
| V ₄₉ (pu) | 1.080453 | 1.087637 | 1.048898 | 1.0535 | 1.0528 | 1.0600 | 1.0444 | 1.0836 | 0.9838 |
| V ₅₄ (pu) | 1.080622 | 1.086017 | 1.048895 | 1.0291 | 1.0146 | 1.0388 | 1.0379 | 0.9764 | 0.9637 |

| | | | | | | | | | |
|--------------------------|----------|----------|----------|--------|--------|--------|---------|---------|---------|
| V ₅₅ (pu) | 1.082479 | 1.087637 | 1.049464 | 1.0285 | 1.0149 | 1.0380 | 0.9907 | 1.0103 | 0.9716 |
| V ₅₆ (pu) | 1.081206 | 1.087637 | 1.048895 | 1.0286 | 1.0162 | 1.0382 | 1.0333 | 0.9536 | 1.0250 |
| V ₅₉ (pu) | 1.081425 | 1.087637 | 1.049021 | 1.0478 | 1.0046 | 1.0600 | 1.0099 | 0.9672 | 1.0003 |
| V ₆₁ (pu) | 1.082719 | 1.086914 | 1.049619 | 1.0406 | 1.0468 | 1.0600 | 1.0925 | 1.0938 | 1.0771 |
| V ₆₂ (pu) | 1.083514 | 1.085743 | 1.049477 | 1.0346 | 1.0547 | 1.0559 | 1.0393 | 1.0978 | 1.0480 |
| V ₆₅ (pu) | 1.082064 | 1.085362 | 1.048895 | 1.0600 | 1.0547 | 1.0600 | 0.9998 | 1.0892 | 0.9684 |
| V ₆₆ (pu) | 1.083611 | 1.087637 | 1.049013 | 1.0600 | 1.0572 | 1.0600 | 1.0355 | 1.0861 | 0.9648 |
| V ₆₉ (pu) | 1.081332 | 1.087637 | 1.048895 | 1.0600 | 1.0599 | 1.0600 | 1.1000 | 0.9665 | 0.9574 |
| V ₇₀ (pu) | 1.085016 | 1.087637 | 1.048895 | 1.0371 | 1.0297 | 1.0377 | 1.0992 | 1.0783 | 0.9765 |
| V ₇₂ (pu) | 1.080457 | 1.087637 | 1.048895 | 1.0390 | 0.9832 | 1.0430 | 1.0014 | 0.9506 | 1.0243 |
| V ₇₃ (pu) | 1.08344 | 1.087637 | 1.048895 | 1.0411 | 1.0030 | 1.0374 | 1.0111 | 0.9722 | 0.9651 |
| V ₇₄ (pu) | 1.077322 | 1.087637 | 1.049577 | 1.0235 | 1.0239 | 1.0275 | 1.0476 | 0.9713 | 1.0733 |
| V ₇₆ (pu) | 1.083105 | 1.087637 | 1.048895 | 1.0107 | 0.9474 | 1.0253 | 1.0211 | 0.9602 | 1.0302 |
| V ₇₇ (pu) | 1.082106 | 1.087637 | 1.048895 | 1.0297 | 1.0311 | 1.0473 | 1.0187 | 1.0781 | 1.0275 |
| V ₈₀ (pu) | 1.081767 | 1.087637 | 1.048895 | 1.0389 | 1.0510 | 1.0600 | 1.0462 | 1.0788 | 0.9857 |
| V ₈₅ (pu) | 1.080431 | 1.087637 | 1.049744 | 1.0514 | 1.0070 | 1.0600 | 1.0491 | 0.9568 | 0.9836 |
| V ₈₇ (pu) | 1.082422 | 1.087637 | 1.048895 | 1.0417 | 0.9421 | 1.0600 | 1.0426 | 0.9642 | 1.0882 |
| V ₈₉ (pu) | 1.083053 | 1.087637 | 1.048963 | 1.0600 | 1.0562 | 1.0600 | 1.0955 | 0.9748 | 0.9895 |
| V ₉₀ (pu) | 1.082293 | 1.087637 | 1.04913 | 1.0340 | 1.0389 | 1.0445 | 1.0417 | 1.0248 | 0.9905 |
| V ₉₁ (pu) | 1.081724 | 1.08608 | 1.048895 | 1.0374 | 1.0198 | 1.0496 | 1.0032 | 0.9615 | 1.0288 |
| V ₉₂ (pu) | 1.081534 | 1.087637 | 1.048895 | 1.0470 | 1.0167 | 1.0600 | 1.0927 | 0.9568 | 0.9760 |
| V ₉₉ (pu) | 1.082929 | 1.087637 | 1.048895 | 1.0309 | 1.0588 | 1.0560 | 1.0433 | 0.9540 | 1.0880 |
| V ₁₀₀ (pu) | 1.083526 | 1.087637 | 1.049271 | 1.0257 | 1.0332 | 1.0600 | 1.0786 | 0.9584 | 0.9617 |
| V ₁₀₃ (pu) | 1.079498 | 1.087637 | 1.049037 | 1.0113 | 1.0141 | 1.0600 | 1.0266 | 1.0162 | 0.9611 |
| V ₁₀₄ (pu) | 1.082023 | 1.087637 | 1.04937 | 0.9949 | 1.0063 | 1.0518 | 0.9808 | 1.0992 | 1.0125 |
| V ₁₀₅ (pu) | 1.083416 | 1.087637 | 1.048941 | 0.9923 | 0.9945 | 1.0517 | 1.0163 | 0.9694 | 1.0684 |
| V ₁₀₇ (pu) | 1.079004 | 1.087637 | 1.049361 | 0.9800 | 0.9487 | 1.0389 | 0.9987 | 0.9656 | 0.9769 |
| V ₁₁₀ (pu) | 1.083079 | 1.087637 | 1.048952 | 0.9984 | 1.0441 | 1.0508 | 1.0218 | 1.0873 | 1.0414 |
| V ₁₁₁ (pu) | 1.08312 | 1.086442 | 1.048895 | 1.0080 | 0.9743 | 1.0600 | 0.9852 | 1.0375 | 0.9790 |
| V ₁₁₂ (pu) | 1.080024 | 1.08502 | 1.049312 | 0.9823 | 0.9863 | 1.0358 | 0.9500 | 1.0920 | 0.9764 |
| V ₁₁₃ (pu) | 1.079411 | 1.087637 | 1.049192 | 0.9786 | 0.9771 | 1.0600 | 0.9764 | 1.0753 | 0.9721 |
| V ₁₁₆ (pu) | 1.082748 | 1.087637 | 1.048895 | 1.0473 | 1.0566 | 1.0600 | 1.0372 | 0.9594 | 1.0330 |
| T ₅₋₈ | 0.998432 | 0.989228 | 0.990939 | 0.9900 | 1.0400 | 1.0000 | 1.0659 | 1.0112 | 1.0045 |
| T ₂₅₋₂₆ | 1.001418 | 0.989132 | 0.990341 | 1.1000 | 0.9900 | 1.1000 | 0.9534 | 1.0906 | 1.0609 |
| T ₁₇₋₃₀ | 0.996509 | 0.988683 | 0.990985 | 1.0300 | 1.0800 | 0.9900 | 0.9328 | 1.0033 | 1.0008 |
| T ₃₇₋₃₈ | 0.994913 | 0.989294 | 0.990341 | 1.0100 | 1.0400 | 0.9800 | 1.0884 | 1.0000 | 1.0093 |
| T ₅₉₋₆₃ | 0.996932 | 0.988844 | 0.991035 | 0.9800 | 0.9500 | 0.9800 | 1.0579 | 1.0080 | 0.9922 |
| T ₆₁₋₆₄ | 0.975139 | 0.988621 | 0.990341 | 1.0100 | 1.0200 | 1.0000 | 0.9493 | 1.0326 | 1.0074 |
| T ₆₅₋₆₆ | 0.985599 | 0.988683 | 0.984905 | 0.9400 | 0.9500 | 0.9000 | 0.9975 | 0.9443 | 1.0611 |
| T ₆₈₋₆₉ | 1.00101 | 0.989421 | 0.995988 | 0.9800 | 0.9300 | 0.9500 | 0.9887 | 0.9067 | 0.9307 |
| T ₈₀₋₈₁ | 0.998315 | 0.988447 | 0.993019 | 0.9900 | 1.0300 | 0.9900 | 0.9801 | 0.9673 | 0.9578 |
| Q _{c5} (MVar) | -7.0704 | -0.00581 | -34.8753 | 0.0732 | 0.2064 | -0.4 | 0.0000 | 0.0000 | 0.0000 |
| Q _{C34} (MVar) | 7.765352 | 11.69995 | 8.450712 | 0.0477 | 0.1382 | 0.1400 | 7.4600 | 9.3639 | 11.7135 |
| Q _{C37} (MVar) | -9.21773 | -5.25315 | -9.56137 | 0.1268 | 0.0117 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| Q _{c44} (MVar) | 3.150744 | 5.510977 | 0.999554 | 0.0000 | 0.0081 | 0.0429 | 6.0700 | 9.3078 | 9.8932 |
| Q _{C45} (MVar) | 7.528823 | 7.636399 | 8.649973 | 0.0505 | 0.0053 | 0.0073 | 3.3300 | 8.6428 | 9.4169 |
| Q _{c46} (MVar) | 0 | 2.804123 | 9.31467 | 0.0669 | 0.0199 | 0.0697 | 6.5100 | 8.9462 | 2.6719 |
| Q _{c48} (MVar) | 1.644068 | 9.910066 | 14.99576 | 0.0321 | 0.1461 | 0.0368 | 4.4700 | 11.8092 | 2.8546 |
| Q _{c74} (MVar) | 10.55347 | 0 | 10.40067 | 0.0000 | 0.0081 | 0.0000 | 9.7200 | 4.6132 | 0.5471 |
| Q _{c79} (MVar) | 3.158644 | 7.858706 | 19.99434 | 0.0000 | 0.1537 | 0.0000 | 14.2500 | 10.5923 | 14.8532 |
| Q _{c82} (MVar) | 14.51898 | 0 | 12.93793 | 0.0000 | 0.0037 | 0.0000 | 17.4900 | 16.4544 | 19.4270 |
| Q _{C83} (MVar) | 7.555023 | 1.153496 | 1.30626 | 0.0260 | 0.0367 | 0.0000 | 4.2800 | 9.6325 | 6.9824 |
| Q _{c105} (MVar) | 0 | 0 | 17.39852 | 0.1995 | 0.0265 | 0.0001 | 12.0400 | 8.9513 | 9.0291 |

| | | | | | | | | | |
|-------------------|---------------|-----------------|---------------|--------|--------|--------|--------|--------|--------|
| Q_{c107} (MVar) | 4.550553 | 0 | 1.371621 | 0.0235 | 0.0587 | 0.0016 | 2.2600 | 5.0426 | 4.9926 |
| Q_{c110} (MVar) | 4.367863 | 3.516079 | 1.336279 | 0.0483 | 0.0486 | 0.0002 | 2.9400 | 5.5319 | 2.2086 |
| Q_{svc} (MVar) | 10.762(20) | 21.654(90) | 11.786(96) | NA | NA | NA | NA | NA | NA |
| Q_{svc} (MVar) | 21.087(68) | 10.767(75) | 8.654(34) | | | | | | |
| Q_{svc} (MVar) | 17.868(106) | 21.867(15) | 21.767(109) | | | | | | |
| X_{TCSC} (pu) | 0.0172(12-16) | 0.1278(96-97) | 0.2171(51-52) | | | | | | |
| X_{TCSC} (pu) | 0.1129(65-68) | 0.0289(106-107) | 0.5442(70-71) | | | | | | |
| X_{TCSC} (pu) | 0.6533(94-93) | 0.4876(28-29) | 0.3215(13-15) | | | | | | |
| P_{Loss} (MW) | 103.54 | 106.62 | 110.645 | | | | | | |

Table 11: Best solutions of all algorithms for IEEE 118 bus system

| Algorithms | Best (pu) | Worst (pu) | Mean (pu) | Std. Dev | % Psave |
|-----------------------|-----------|----------------|----------------|---|--------------|
| ICA [23] | 1.18322 | 1.21527 | 1.18970 | 6.4261×10^{-3} | 11.27 |
| IWO [23] | 1.37295 | 1.56288 | 1.45752 | 9.4227×10^{-2} | -2.95 |
| MICA-IWO [23] | 1.14046 | 1.14976 | 1.14448 | 2.4288×10^{-4} | 14.48 |
| RGA [23] | 1.22140 | 1.26696 | 1.24089 | 1.791×10^{-2} | - |
| CMAES [23] | 1.19275 | 1.21860 | 1.20854 | 8.62×10^{-3} | - |
| MOPSO [23] | 1.19581 | - | - | - | - |
| NSGA-II [23] | 1.19580 | - | - | - | - |
| MNSGA-II [23] | 1.19279 | - | - | - | - |
| DMSDE [23] | 1.15370 | - | 1.16840 | 8.787×10^{-3} | 13.4879 |
| PSO-cf [23] | 1.15821 | - | 1.18827 | 1.7248×10^{-2} | 13.1496 |
| PSO-w [23] | 1.15833 | - | 1.20575 | 2.3574×10^{-2} | 13.1408 |
| AGA [23] | 1.23964 | - | 1.27827 | 2.0613×10^{-2} | 17.0438 |
| MVMO [23] | 1.15793 | 1.19358 | 1.16820 | 7.682×10^{-3} | - |
| PSO [23] | 1.20897 | 1.35372 | 1.25487 | 3.1634×10^{-2} | - |
| DE [23] | 1.25025 | 1.30229 | 1.27442 | 1.1337×10^{-2} | - |
| JADE [23] | 1.19161 | 1.32035 | 1.22677 | 3.0467×10^{-2} | - |
| JADE-vPS [23] | 1.19201 | 1.33344 | 1.25575 | 3.8943×10^{-2} | - |
| CGA [23] | 1.39415 | 1.49009 | 1.43548 | 2.6026×10^{-2} | - |
| AGA [23] | 1.24209 | 1.31078 | 1.27701 | 1.836×10^{-2} | - |
| PSO-w [23] | 1.15815 | 1.18214 | 1.16771 | 6.8971×10^{-3} | - |
| PSO-cf [23] | 1.15642 | 1.18058 | 1.16202 | 6.1864×10^{-3} | - |
| CLPSO [23] | 1.23152 | 1.25499 | 1.24080 | 6.4325×10^{-3} | - |
| SPSO-07 [23] | 1.39275 | 1.50244 | 1.46266 | 2.653×10^{-2} | - |
| L-DE [23] | 1.51009 | 1.76614 | 1.62315 | 8.2443×10^{-2} | - |
| L-SACP-DE [23] | 1.41799 | 1.76812 | 1.60679 | 1.0643×10^{-1} | - |
| L-SaDE [23] | 1.16906 | 1.18862 | 1.17598 | 5.4041×10^{-3} | - |
| SOA [12] | 1.14950 | 1.16347 | 1.15674 | 3.5908×10^{-3} | - |
| ALO (proposed) | 1.1064 | 1.12065 | 1.11233 | 3.2083×10^{-3} | 16.36 |
| WOA (proposed) | 1.0662 | 1.08467 | 1.07865 | 3.1434×10^{-3} | 19.40 |
| SCA (proposed) | 1.0354 | 1.05321 | 1.04566 | 2.3256×10^{-3} | 21.72 |

SCA based reactive power dispatch schedule for the trial system of power loss minimization objective is presented in Table 10 and the results obtained are compared to ICA [23]; IWO [23]; MICA-IWO [23]; GSA [19]; PSO [19]; CLPSO [19], ALO and WOA. This table proves that the SCA yield optimal loss as compared to other algorithms. Table 11 records the statistical comparison of effects obtained from SCA with existing results presented in the literature. From this table, noted that the standard deviation and median values are quite acceptable for SCA. Good convergence profile of the SCA may be noticed from this Fig. 12 by way of its ability to achieve the approximate optimal solution.

3. Conclusion

In the proposed work, three newest optimization techniques (SCA, WOA and ALO) are applied for effective co-ordination of series and shunt FACTS devices with the control variables present in a connected power system. To obtain reactive power optimization with FACTS devices, the execution of three algorithms has been carried out on the IEEE 14-bus, 57-bus, and large 118-bus schemes. SCA was one among various optimization methods that creates better outcomes compared with existing literatures. Maintenance of voltage profile, reduction of power loss, and optimization of reactive power have been facilitated by the algorithm. Hence SCA may be seen as a very good optimization technique in the field of power system planning and future research credentials.

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